

DATA MINING

LECTURE 7

Clustering

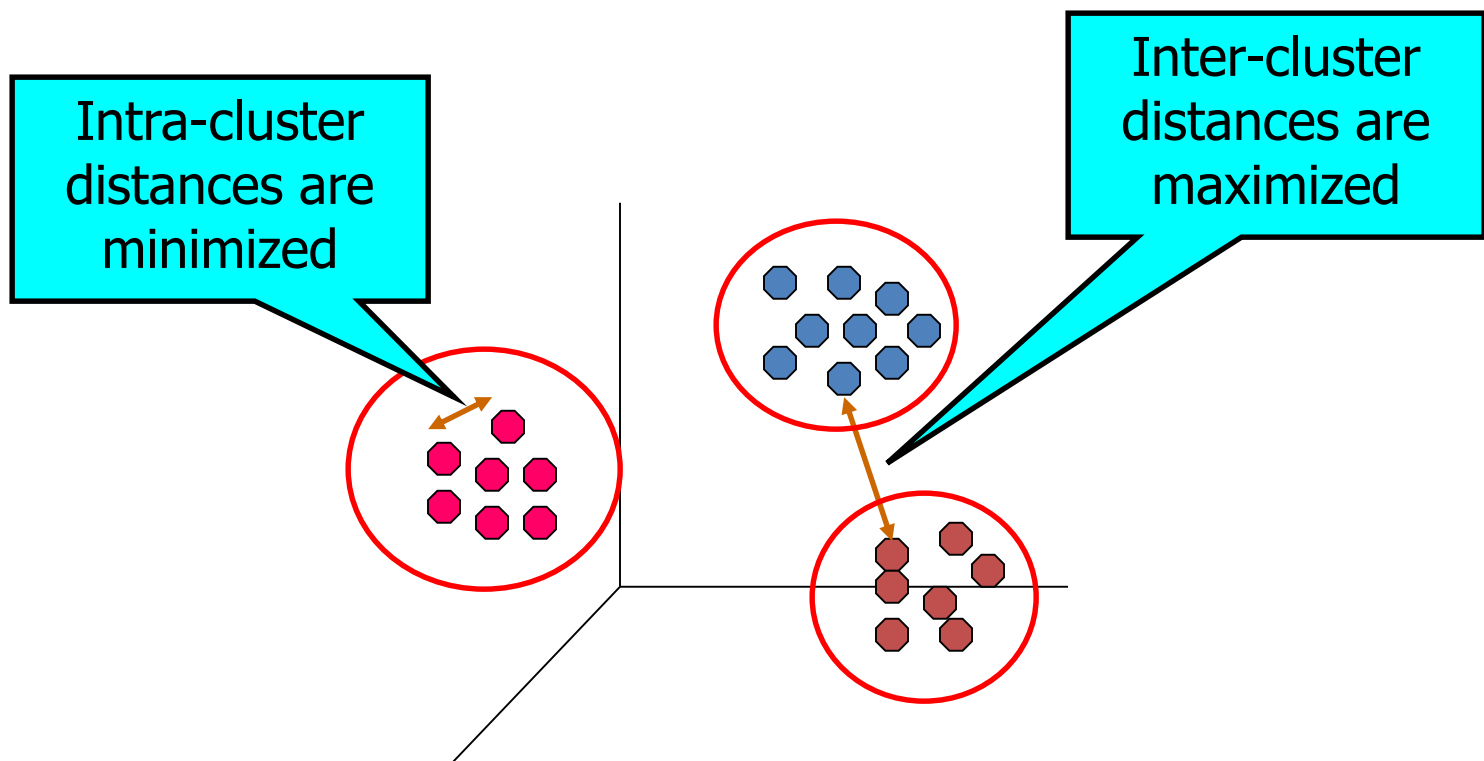
The k-means algorithm

Hierarchical Clustering

The DBSCAN algorithm

What is a Clustering?

- In general a **grouping** of objects such that the objects in a **group** (**cluster**) are similar (or related) to one another and different from (or unrelated to) the objects in other groups



Applications of Cluster Analysis

- **Understanding**

- **Group** related **documents** for browsing, **genes and proteins** that have similar functionality, **stocks** with similar price fluctuations, **users** with same behavior

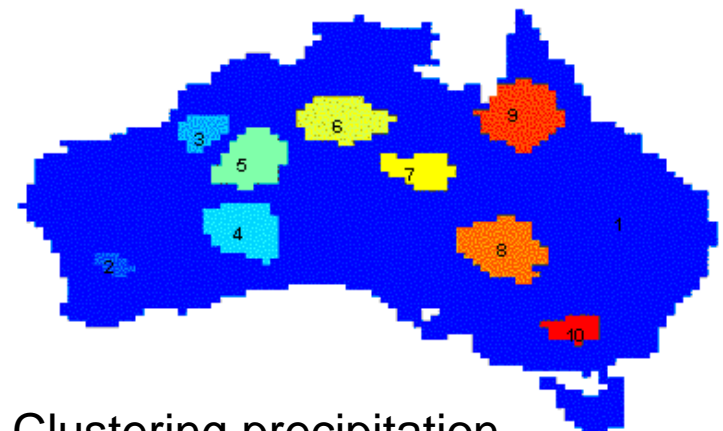
- **Summarization**

- Reduce the size of large data sets

- **Applications**

- Recommendation systems
- Search Personalization

| | <i>Discovered Clusters</i> | <i>Industry Group</i> |
|----------|---|-----------------------|
| 1 | Applied-Matl-DOWN,Bay-Network-DOWN,3-COM-DOWN, Cabletron-Sys-DOWN,CISCO-DOWN,HP-DOWN, DSC-Comm-DOWN,INTEL-DOWN,LSI-Logic-DOWN, Micron-Tech-DOWN,Texas-Inst-DOWN,Tellabs-Inc-DOWN, Natl-Semiconduct-DOWN,Oracl-DOWN,SGI-DOWN, Sun-DOWN | Technology1-DOWN |
| 2 | Apple-Comp-DOWN,Autodesk-DOWN,DEC-DOWN, ADV-Micro-Device-DOWN,Andrew-Corp-DOWN, Computer-Assoc-DOWN,Circuit-City-DOWN, Compaq-DOWN, EMC-Corp-DOWN, Gen-Inst-DOWN, Motorola-DOWN,Microsoft-DOWN,Scientific-Atl-DOWN | Technology2-DOWN |
| 3 | Fannie-Mae-DOWN,Fed-Home-Loan-DOWN, MBNA-Corp-DOWN,Morgan-Stanley-DOWN | Financial-DOWN |
| 4 | Baker-Hughes-UP,Dresser-Inds-UP,Halliburton-HLD-UP, Louisiana-Land-UP,Phillips-Petro-UP,Unocal-UP, Schlumberger-UP | Oil-UP |



Clustering precipitation in Australia

Early applications of cluster analysis

- John Snow, London 1854

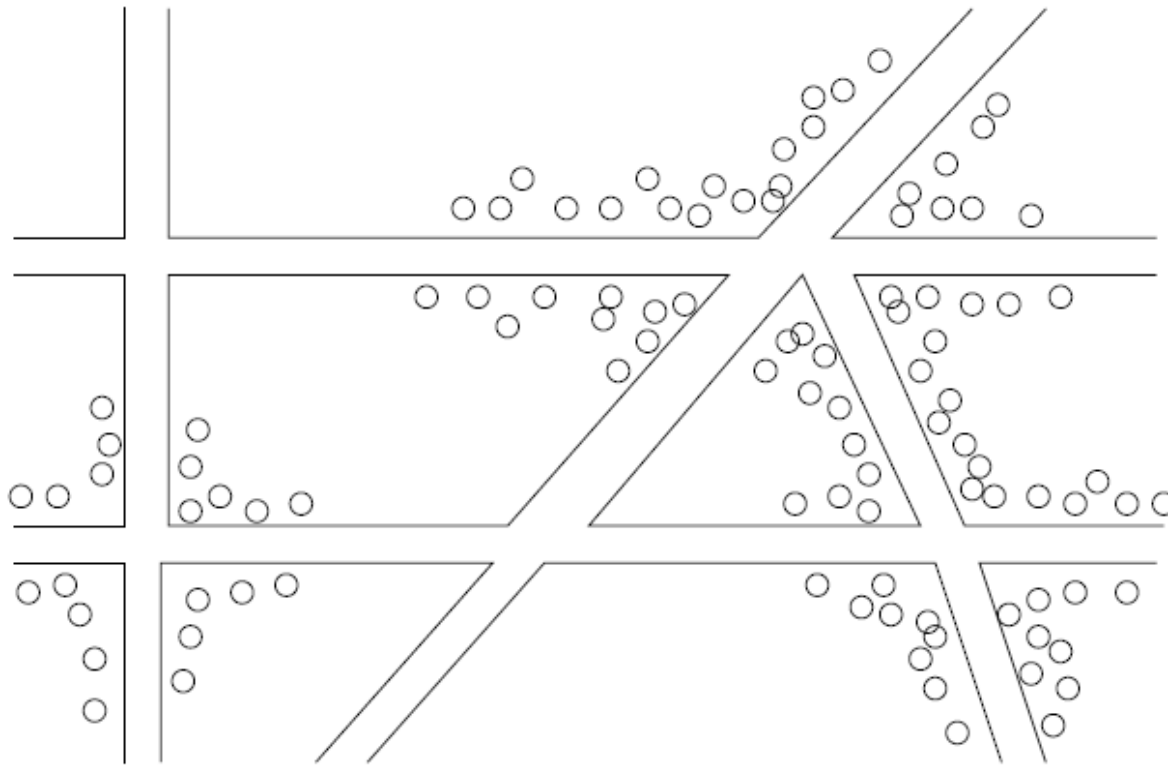
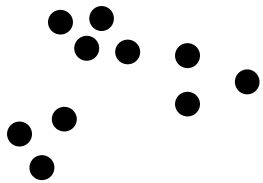
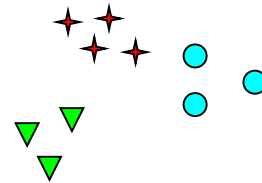
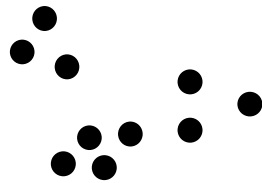


Figure 1.1: Plotting cholera cases on a map of London

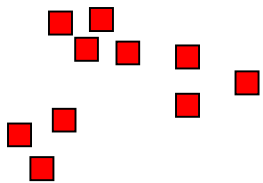
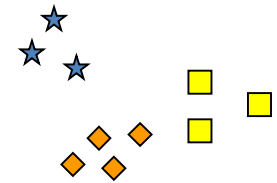
Notion of a Cluster can be Ambiguous



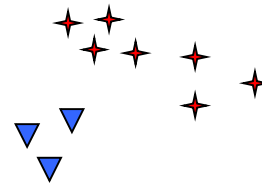
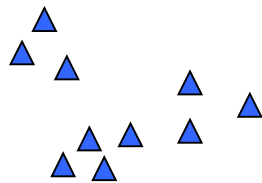
How many clusters?



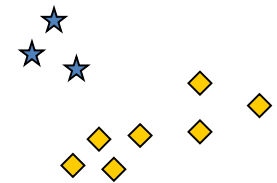
Six Clusters



Two Clusters



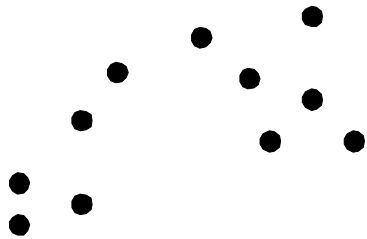
Four Clusters



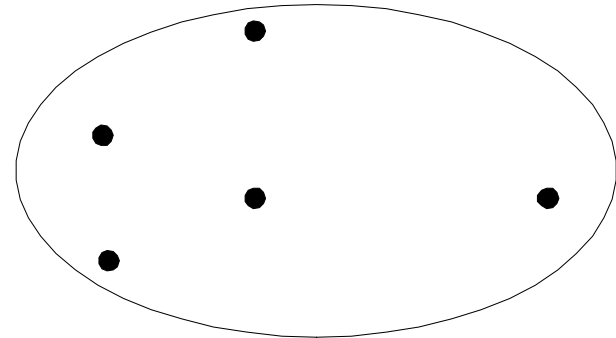
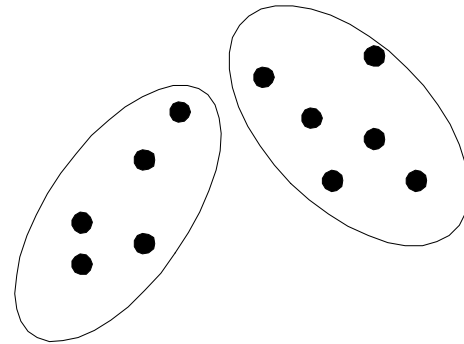
Types of Clusterings

- A **clustering** is a set of **clusters**
- Important distinction between **hierarchical** and **partitional** sets of clusters
- **Partitional** Clustering
 - A division data objects into subsets (**clusters**) such that each data object is in exactly one subset
- **Hierarchical** clustering
 - A set of nested clusters organized as a hierarchical tree

Partitional Clustering

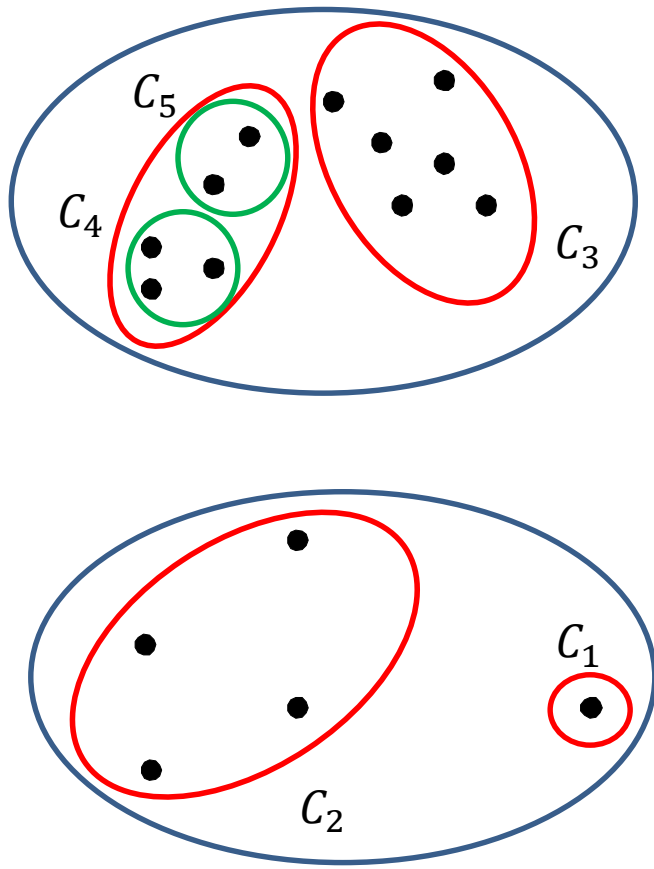


Original Points

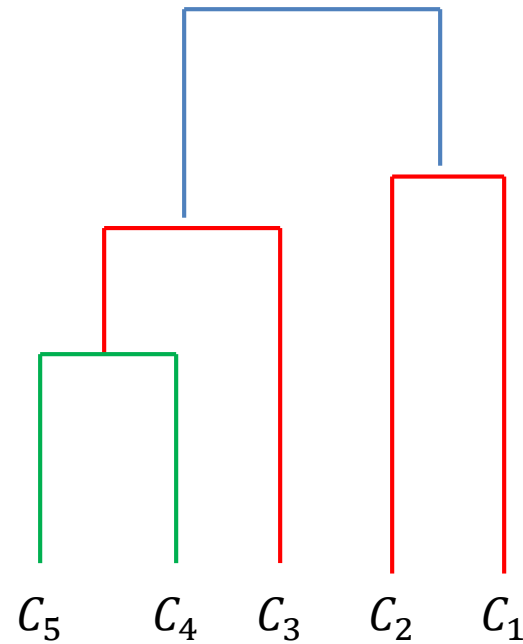


A Partitional Clustering

Hierarchical Clustering



Hierarchical Clustering



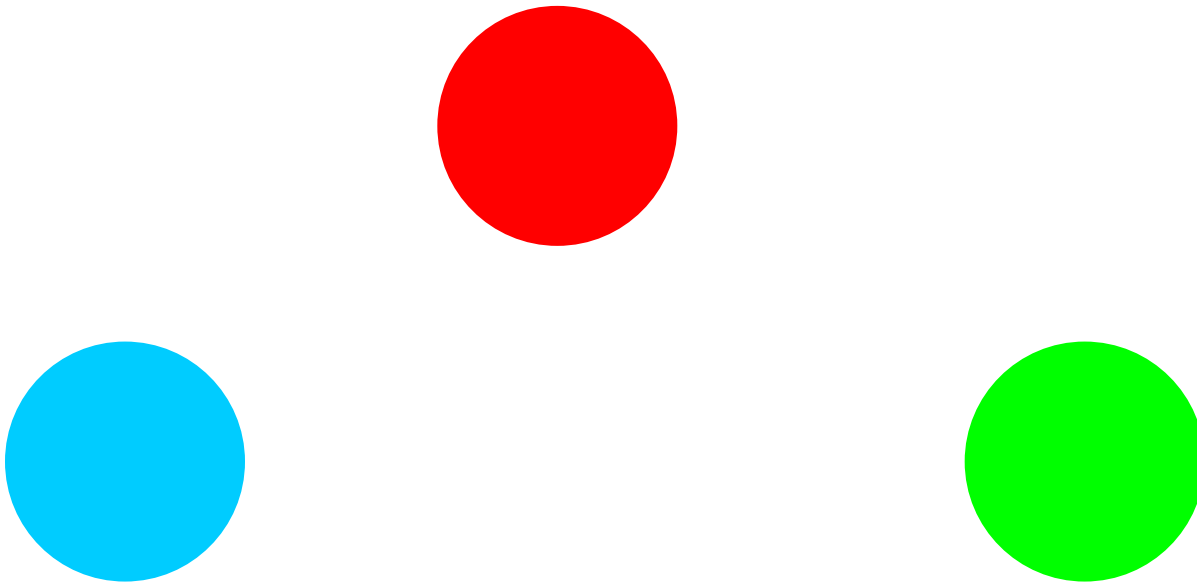
Hierarchical Clustering dendrogram

Other types of clustering

- **Exclusive** (or **non-overlapping**) versus **non-exclusive** (or **overlapping**)
 - In non-exclusive clusterings, points may belong to multiple clusters.
 - Points that belong to multiple classes, or 'border' points
- **Fuzzy** (or **soft**) versus **non-fuzzy** (or **hard**)
 - In fuzzy clustering, a point belongs to every cluster with some weight between 0 and 1
 - Weights usually must sum to 1 (often interpreted as **probabilities**)
- **Partial** versus **complete**
 - In some cases, we only want to cluster some of the data

Clustering objectives

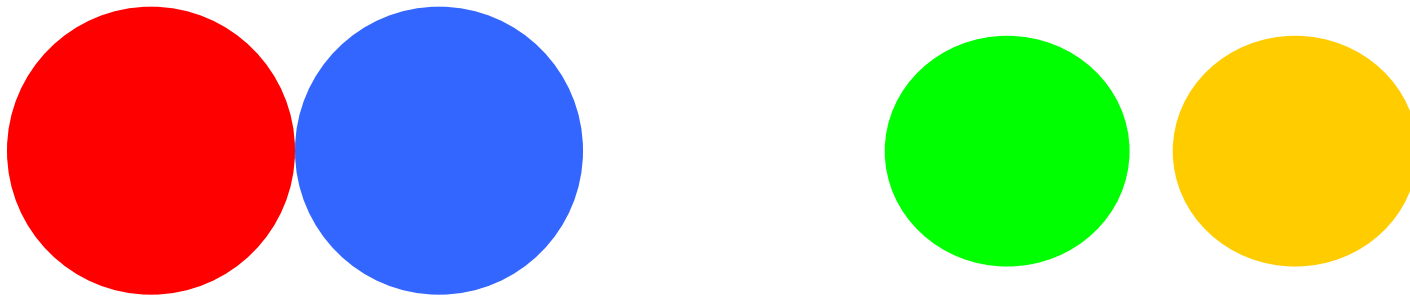
- **Well-Separated Clusters:**
 - A cluster is a set of points such that any point in a cluster is closer (or more similar) to every other point in the cluster than to any point not in the cluster.



3 well-separated clusters

Clustering objectives

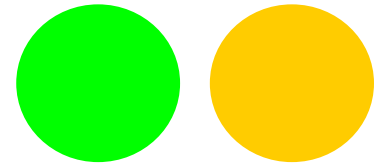
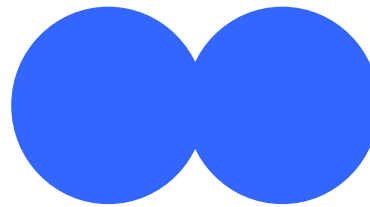
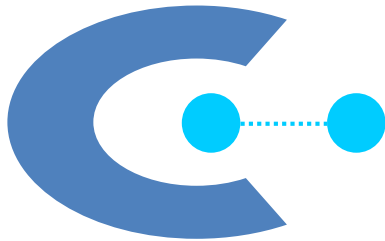
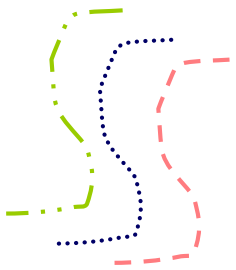
- Center-based
 - A cluster is a set of objects such that an object in a cluster is **closer** (more **similar**) to the “center” of a cluster, than to the center of any other cluster
 - The center of a cluster is often a **centroid**, the minimizer of distances from all the points in the cluster, or a **medoid**, the most “representative” point of a cluster



4 center-based clusters

Clustering objectives

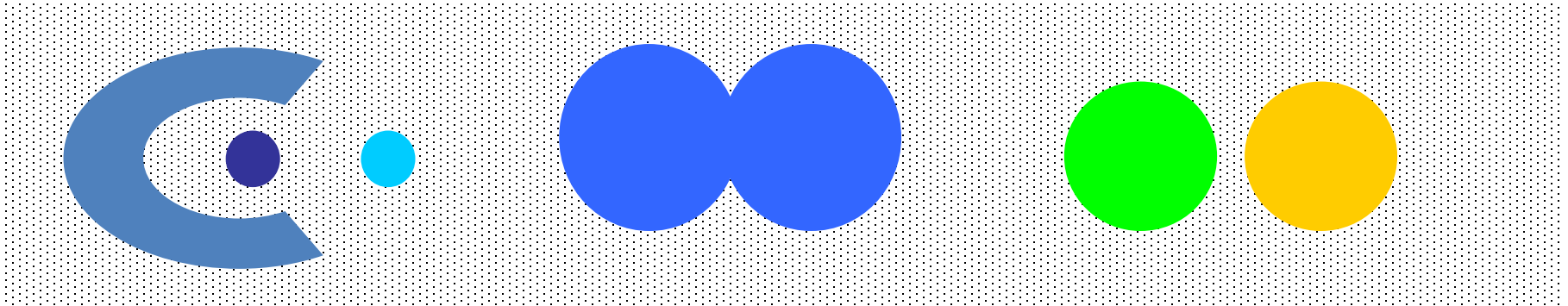
- Contiguous Cluster (Nearest neighbor or Transitive)
 - A cluster is a set of points such that a point in a cluster is closer (or more similar) to one or more other points in the cluster than to any point not in the cluster.



8 contiguous clusters

Types of Clusters: Density-Based

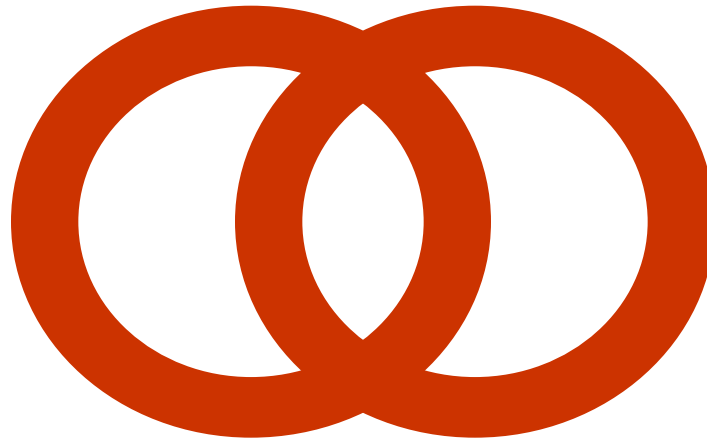
- Density-based
 - A cluster is a dense region of points, which is separated by low-density regions, from other regions of high density.
 - Used when the clusters are irregular or intertwined, and when noise and outliers are present.



6 density-based clusters

Clustering objectives

- **Shared Property or Conceptual Clusters**
 - Finds clusters that share some common property or represent a particular concept.
 -



2 Overlapping Circles

Types of Clusters: Objective Function

- Clustering as an **optimization problem**
 - Finds clusters that minimize or maximize an **objective function**.
 - Consider all possible ways of dividing the points into clusters and compute the **'goodness'** of each clustering using the objective function to find the best one.
 - Usually, finding the best is NP-hard (no polynomial algorithm).
 - Can have **global** or **local** objectives.
 - Hierarchical clustering algorithms typically have local objectives
 - Partitional algorithms typically have global objectives
 - A variation of the global objective function approach is to **fit** the data to a **parameterized (probabilistic) model**.
 - The **parameters** for the model are determined from the data, and they determine the clustering
 - E.g., **Mixture models** assume that the data is a 'mixture' of a number of statistical distributions.

Clustering Algorithms

- K-means and its variants
- Hierarchical clustering
- DBSCAN

K-MEANS

K-means Clustering

- Partitional clustering approach
- Each cluster is associated with a **centroid** (center point)
- Each point is assigned to the cluster with the **closest** centroid
- Number of clusters, **K**, must be specified
- The **objective** is find **K centroids** and the **assignment** of **points to clusters/centroids** so as to **minimize the sum of distances** of the points to their respective **centroid**

K-means Clustering

- **Problem:** Given a set X of n objects and an integer K , group the points into K clusters $C = \{C_1, C_2, \dots, C_k\}$ such that

$$Cost(C) = \sum_{i=1}^k \sum_{x \in C_i} dist(x, c_i)$$

is **minimized**, where c_i is the **centroid** of the points in cluster C_i

- Note: We need to find **both** the **grouping** into clusters **and** the **centroids** per cluster.

K-means Clustering

- Most common definition is with euclidean distance, minimizing the **Sum of Squares Error (SSE)** function
 - Sometimes K-means is defined like that
- **Problem:** Given a set X of n points in a d -dimensional space and an integer K group the points into K clusters $C = \{C_1, C_2, \dots, C_k\}$ such that

$$Cost(C) = \sum_{i=1}^k \sum_{x \in C_i} (x - c_i)^2$$

is **minimized**, where c_i is the **mean** of the points in cluster C_i

Sum of Squares Error (SSE)

Complexity of the k-means problem

- **NP-hard** if the dimensionality of the data is at least 2 ($d \geq 2$)
 - Finding the best solution in polynomial time is infeasible
- For $d=1$ the problem is solvable in polynomial time (how?)
- A simple iterative algorithm works quite well in practice

K-means Algorithm

- Also known as **Lloyd's algorithm**.
- K-means is sometimes synonymous with this algorithm

1: Select K points as the initial centroids.

2: **repeat**

3: Form K clusters by assigning all points to the closest centroid.

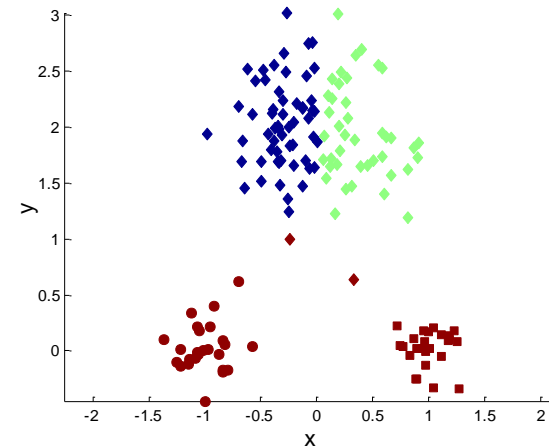
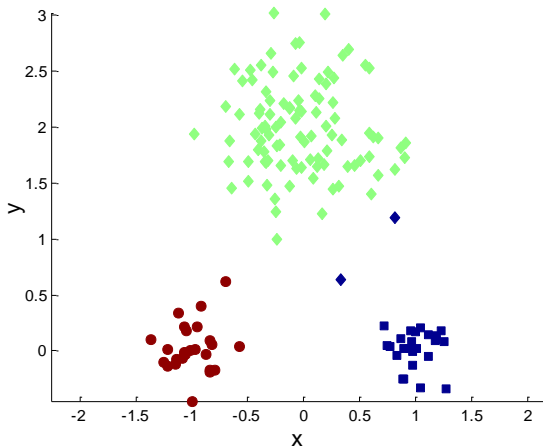
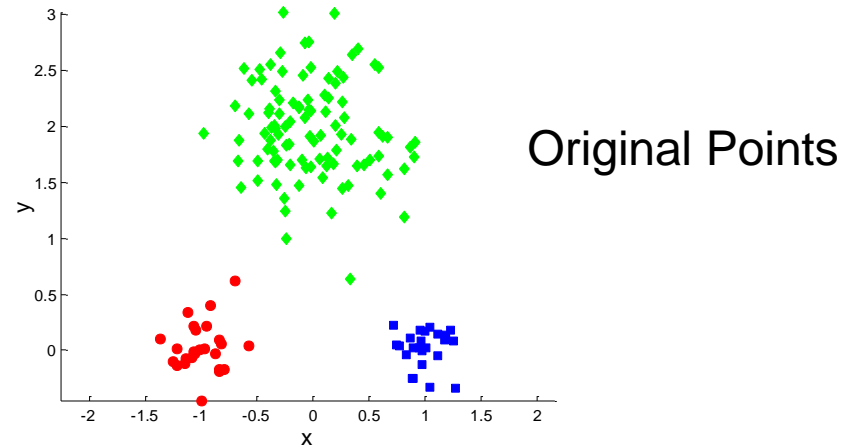
4: Recompute the centroid of each cluster.

5: **until** The centroids don't change

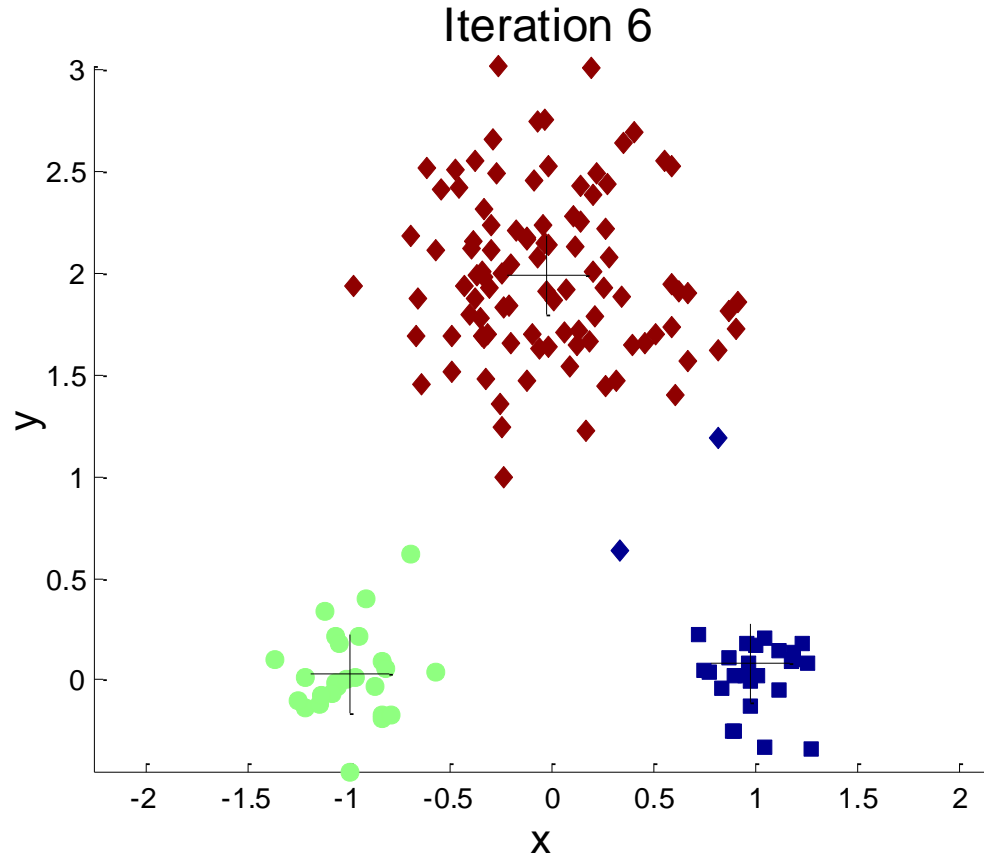
K-means Algorithm – Initialization

- Initial centroids are often chosen **randomly**.
 - Clusters produced vary from one run to another.

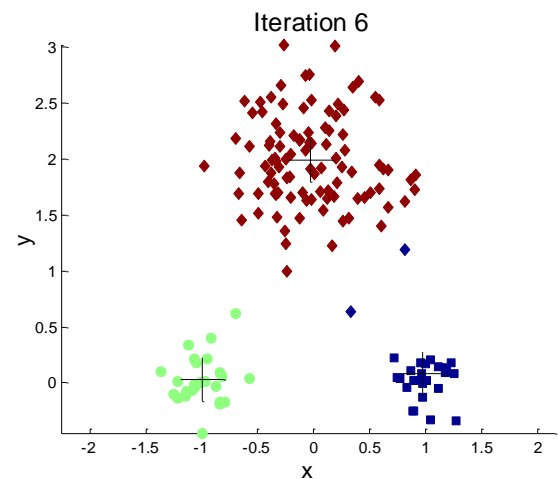
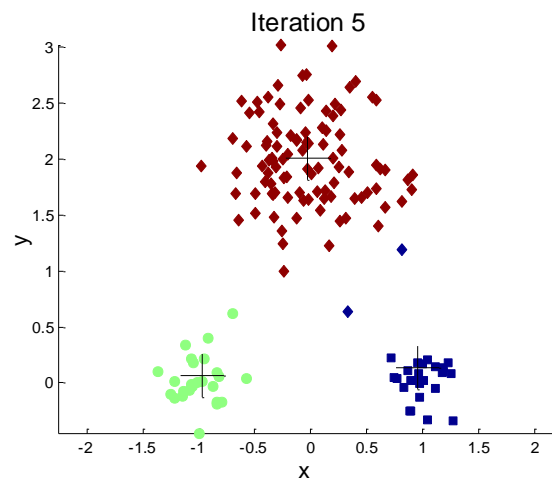
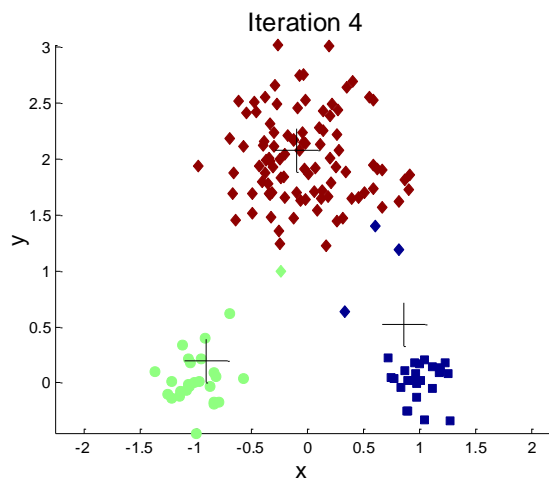
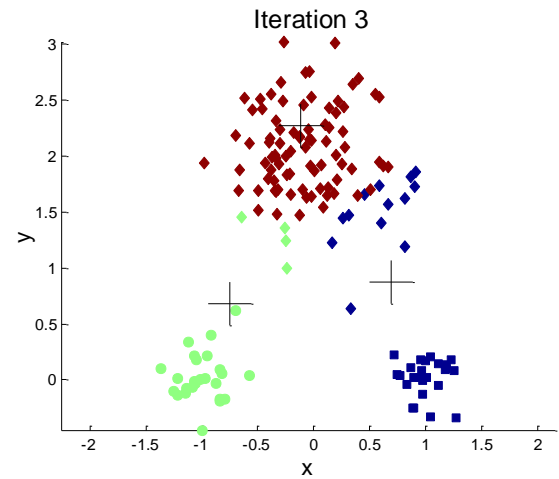
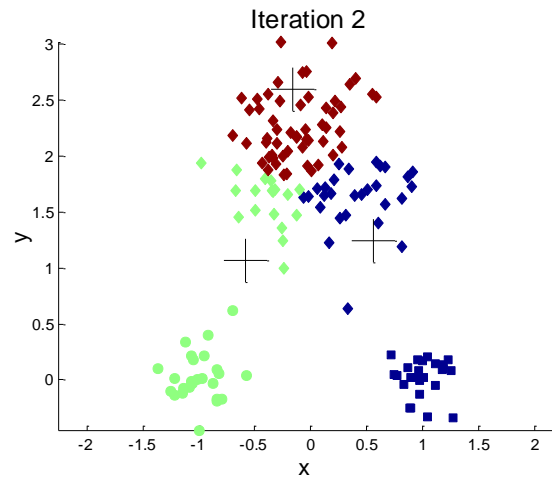
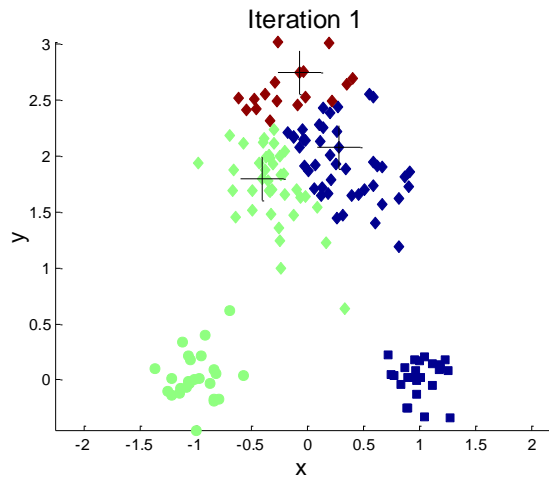
Two different K-means Clusterings



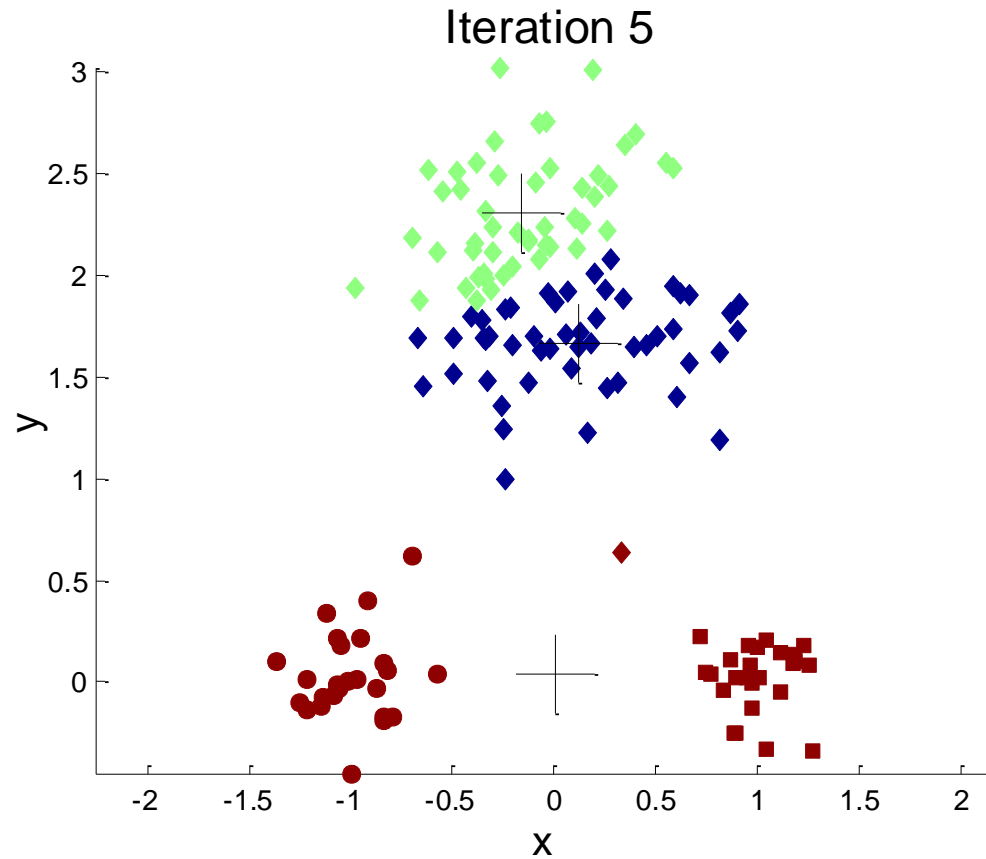
Importance of Choosing Initial Centroids



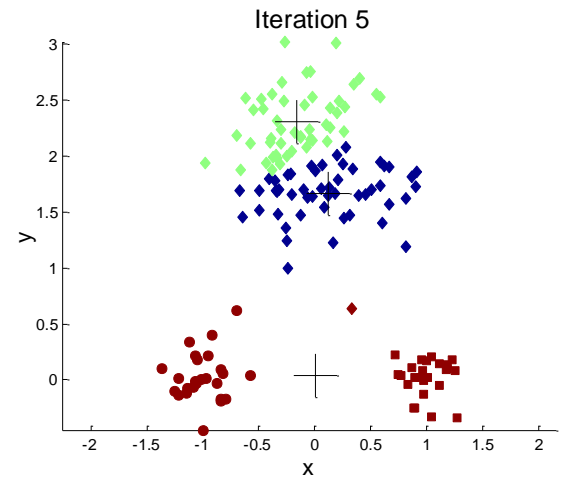
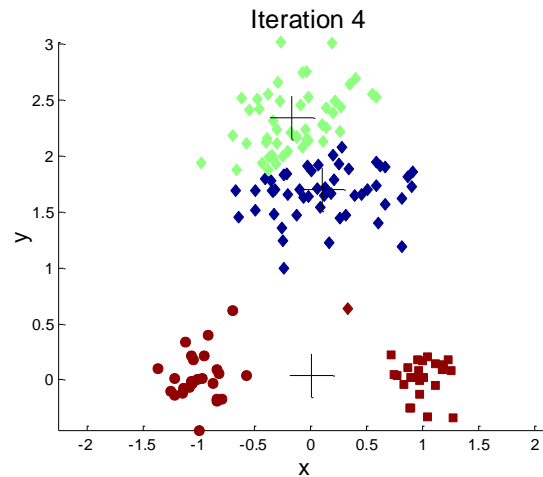
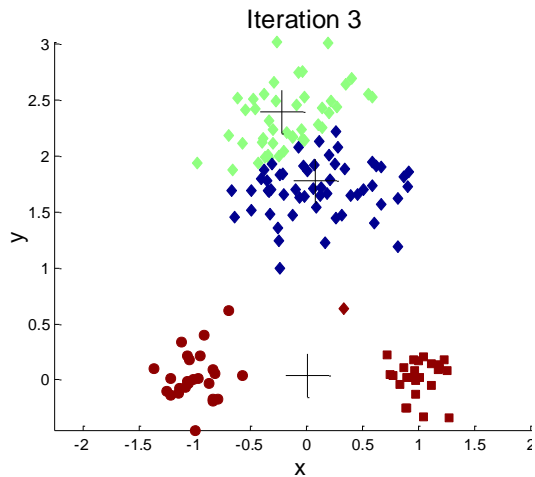
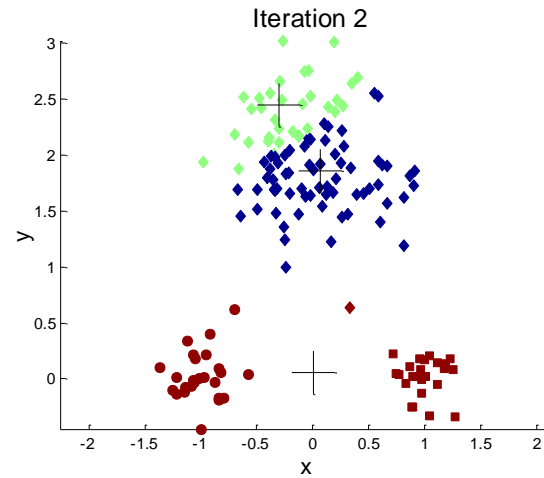
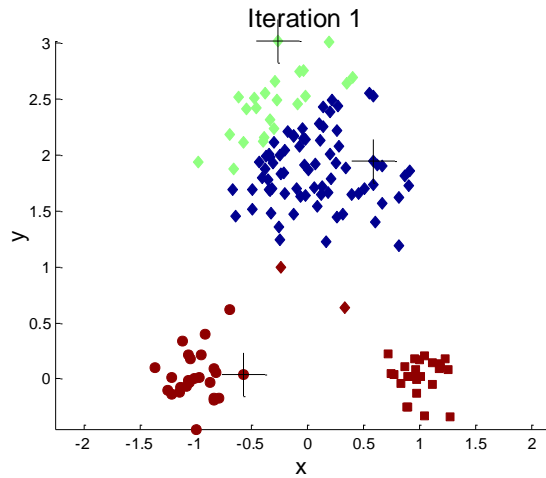
Importance of Choosing Initial Centroids



Importance of Choosing Initial Centroids



Importance of Choosing Initial Centroids ...



Dealing with Initialization

- Do **multiple runs** and select the clustering with the smallest error
- Select original set of points by methods other than random . E.g., pick the most distant (from each other) points as cluster centers (**K-means++** algorithm)

K-means Algorithm – Centroids

- ‘**Closeness**’ is measured by some similarity or distance function
 - E.g., Euclidean distance (SSE), cosine similarity, correlation, etc.
- The **centroid** depends on the distance function
 - The **minimizer** for the distance function
- **Centroid**:
 - The **mean** of the points in the cluster for SSE, and cosine similarity
 - The **median** for Manhattan distance.
- Finding the centroid is not always easy
 - It can be an NP-hard problem for some distance functions
 - E.g., median for multiple dimensions

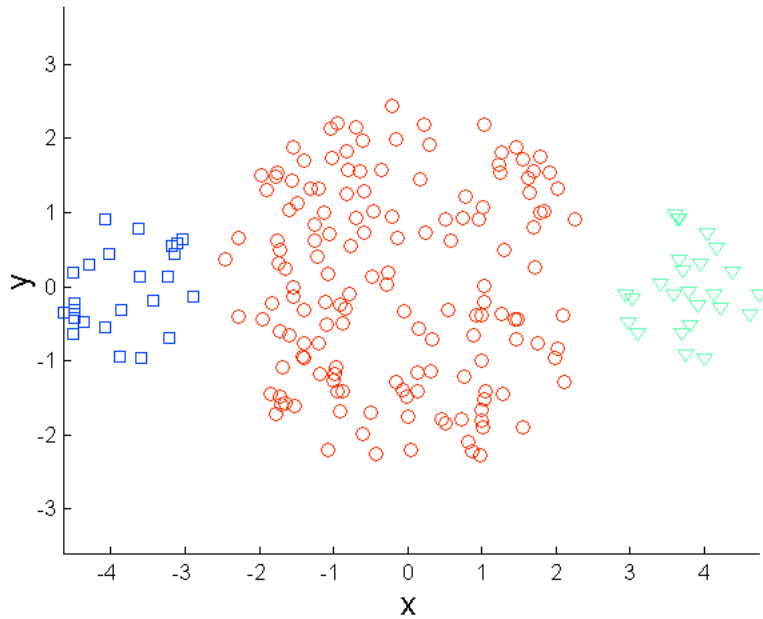
K-means Algorithm – Convergence

- K-means will **converge** for common similarity measures mentioned above.
 - Most of the convergence happens in the first few iterations.
 - Often the stopping condition is changed to ‘**Until relatively few points change clusters**’
- Complexity is $O(n * K * I * d)$
 - n = number of points,
 - K = number of clusters,
 - I = number of iterations,
 - d = dimensionality
- In general a fast and efficient algorithm

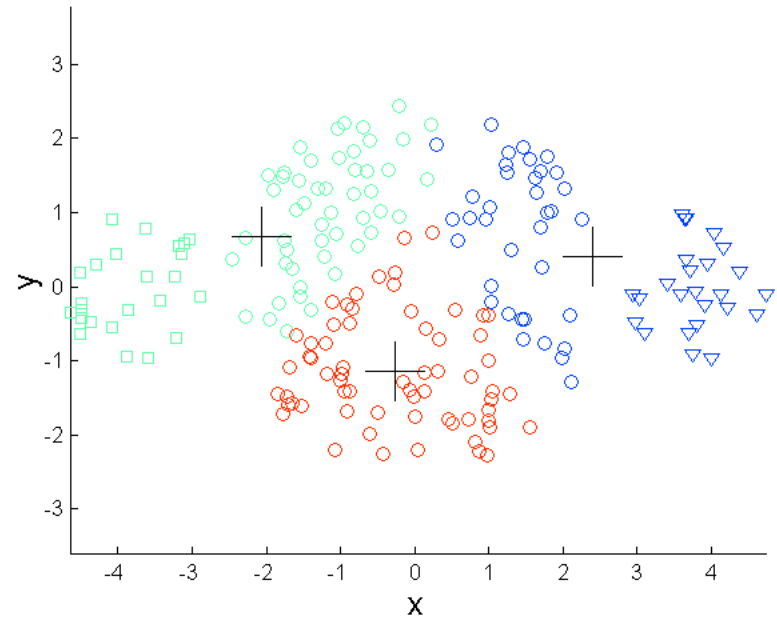
Limitations of K-means

- K-means has problems when clusters are of different:
 - sizes
 - densities
 - **non-globular** shapes
- K-means has problems when the data contains outliers.

Limitations of K-means: Differing Sizes

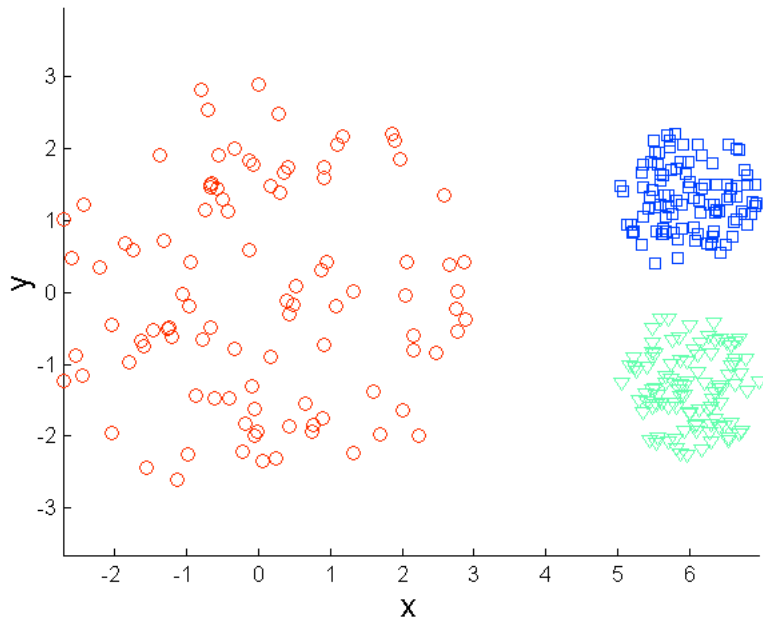


Original Points

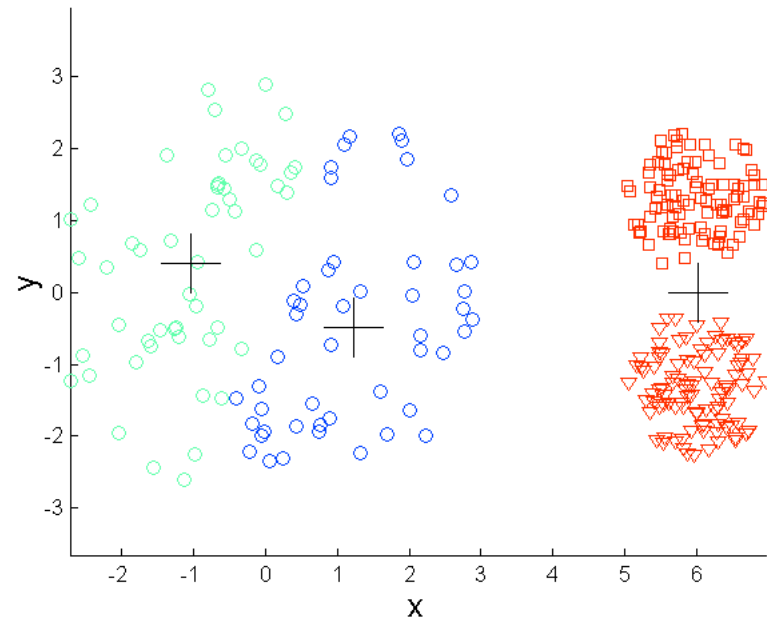


K-means (3 Clusters)

Limitations of K-means: Differing Density

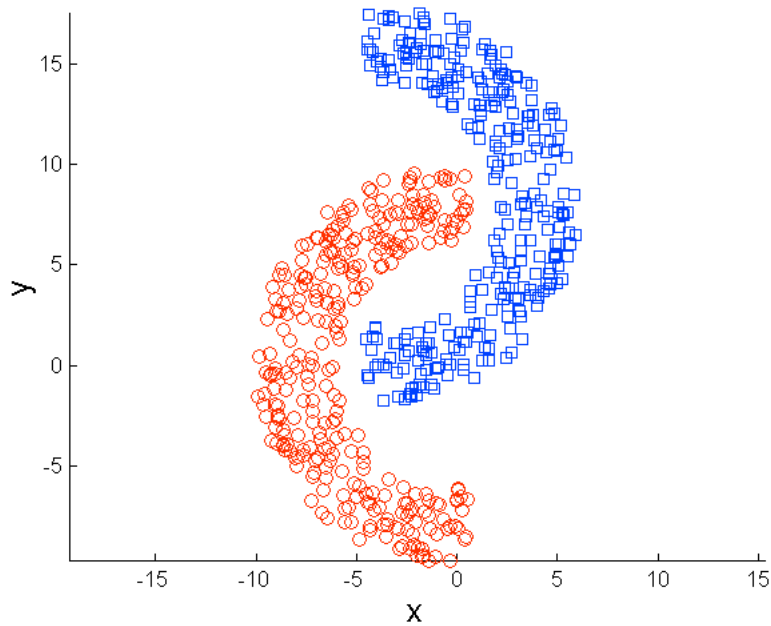


Original Points

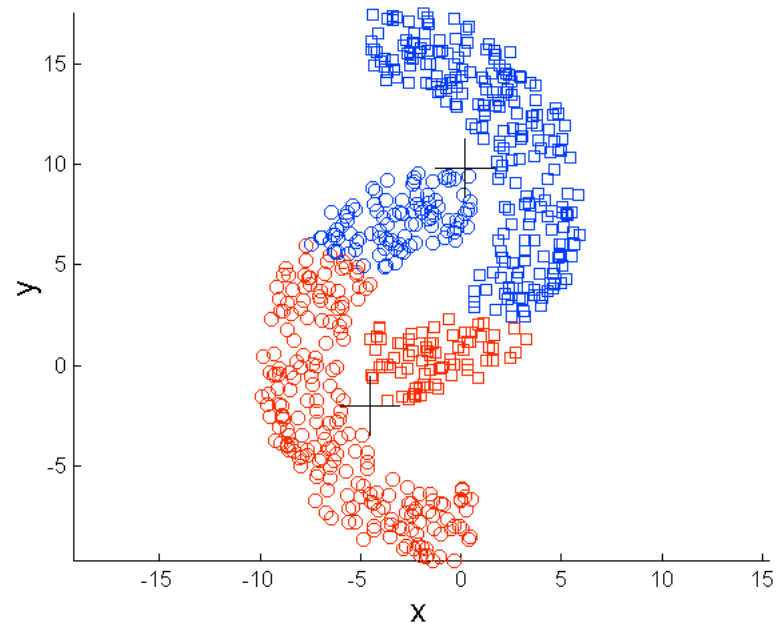


K-means (3 Clusters)

Limitations of K-means: Non-globular Shapes

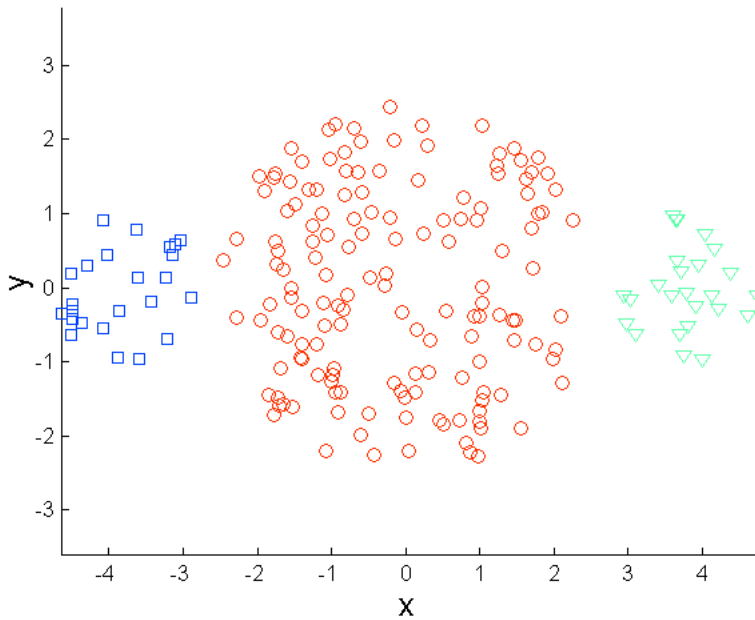


Original Points

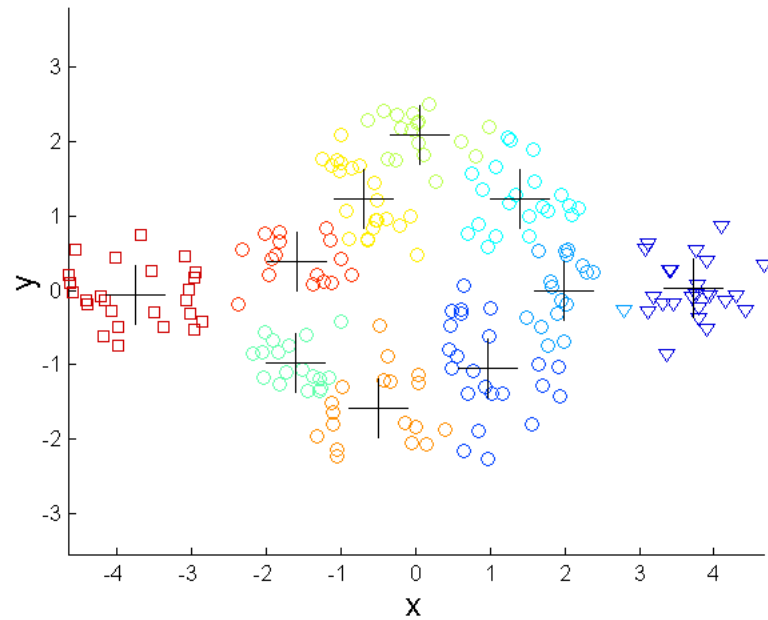


K-means (2 Clusters)

Overcoming K-means Limitations



Original Points

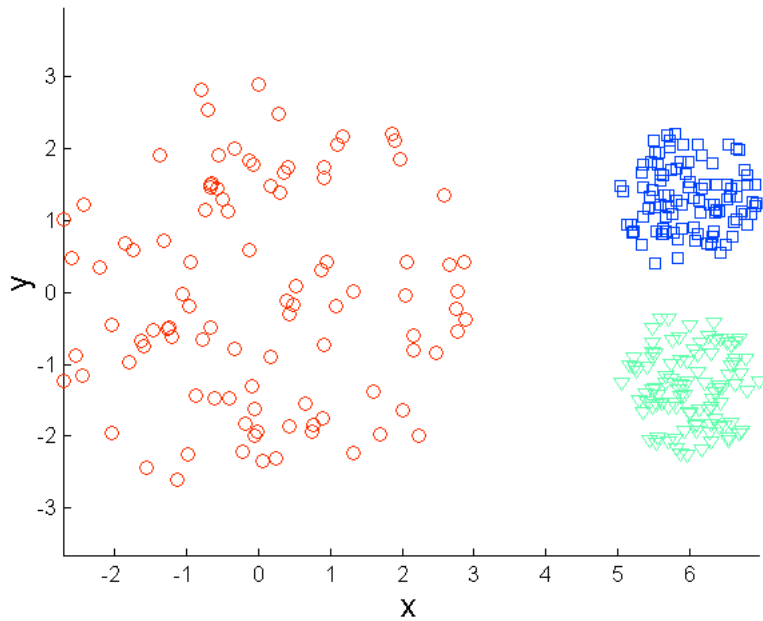


K-means Clusters

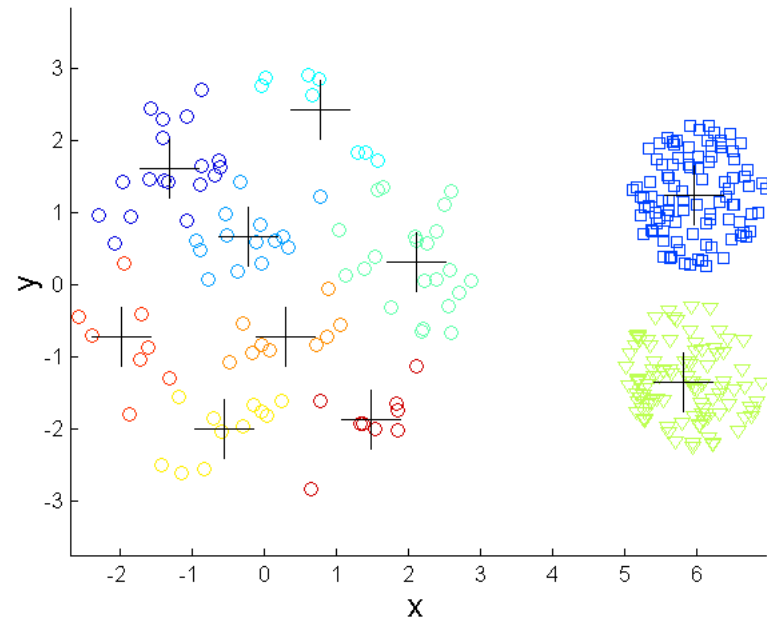
One solution is to use many clusters.

Find parts of clusters, but need to put together.

Overcoming K-means Limitations

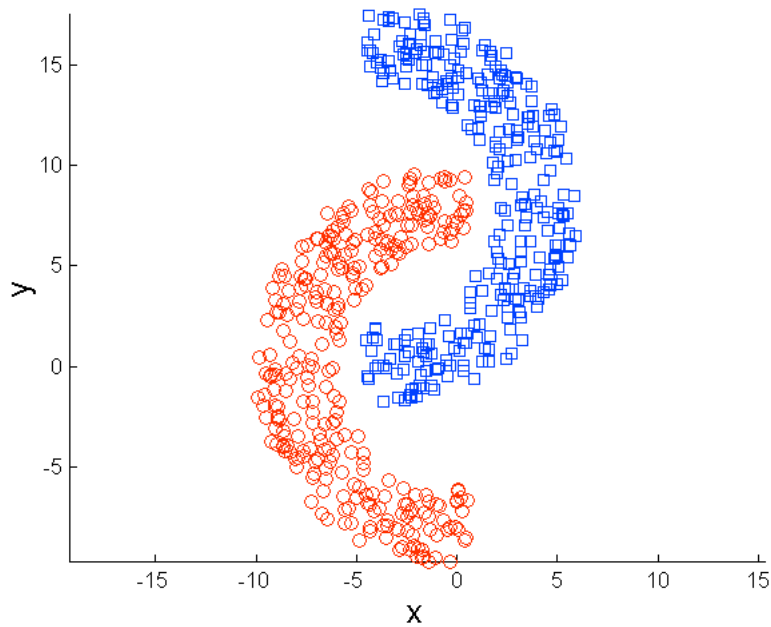


Original Points

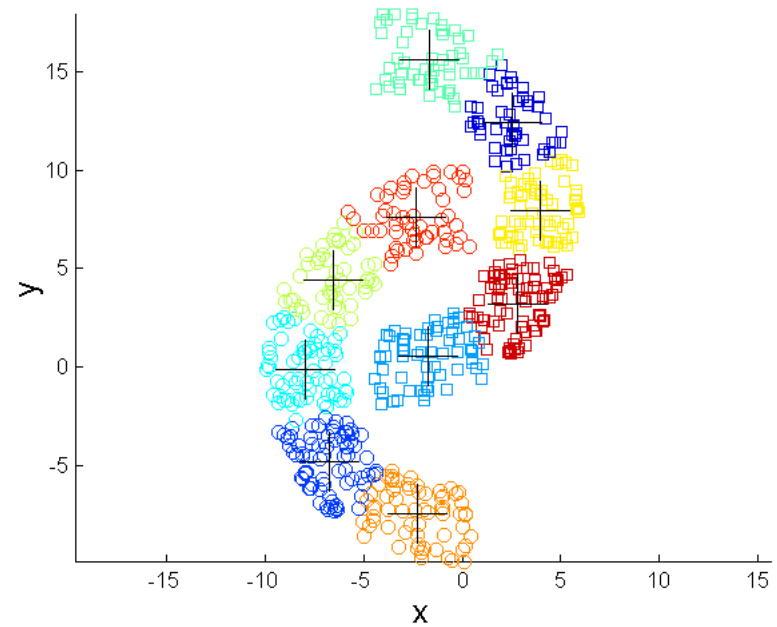


K-means Clusters

Overcoming K-means Limitations



Original Points



K-means Clusters

Variations

- **K-medoids**: Similar problem definition as in K-means, but the centroid of the cluster is defined to be one of the points in the cluster (the **medoid**).
- **K-centers**: Similar problem definition as in K-means, but the goal now is to minimize the maximum **diameter** of the clusters
 - diameter of a cluster is maximum distance between any two points in the cluster.

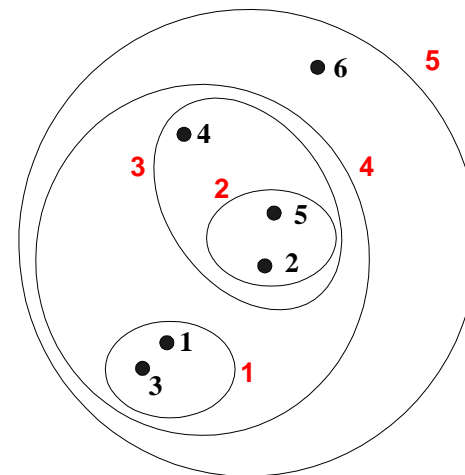
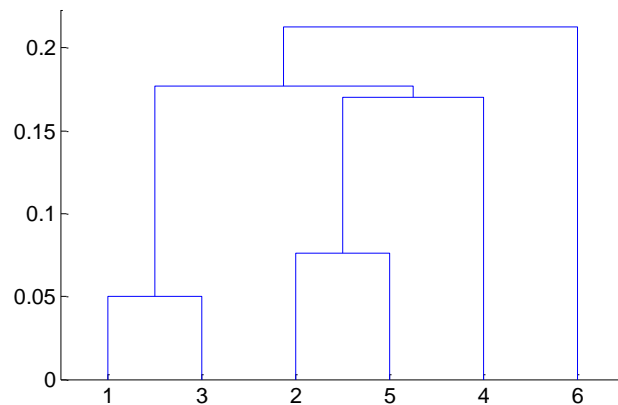
HIERARCHICAL CLUSTERING

Hierarchical Clustering

- Two main types of hierarchical clustering
 - **Agglomerative:**
 - Start with the points as individual clusters
 - At each step, merge the closest pair of clusters until only one cluster (or k clusters) left
 - **Divisive:**
 - Start with one, all-inclusive cluster
 - At each step, split a cluster until each cluster contains a point (or there are k clusters)
- Traditional hierarchical algorithms use a **similarity** or **distance matrix**
 - Merge or split one cluster at a time

Hierarchical Clustering

- Produces a set of nested clusters organized as a hierarchical tree
- Can be visualized as a **dendrogram**
 - A tree like diagram that records the sequences of merges or splits



Strengths of Hierarchical Clustering

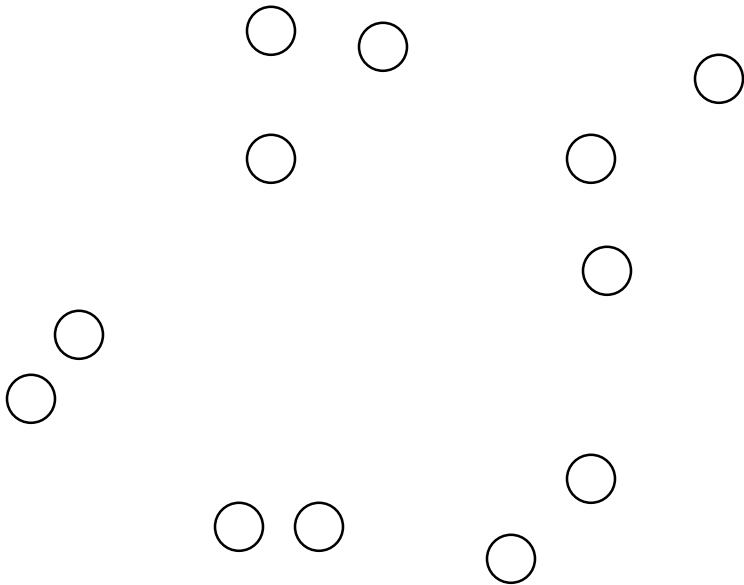
- Do not have to assume any particular number of clusters
 - Any desired number of clusters can be obtained by 'cutting' the dendrogram at the proper level
- Dendrograms **may** correspond to meaningful **taxonomies**
 - Example in biological sciences (e.g., animal kingdom, phylogeny reconstruction, ...)

Agglomerative Clustering Algorithm

- More popular hierarchical clustering technique
- Basic algorithm is straightforward
 1. Compute the **proximity matrix**
 2. Let each data point be a cluster
 3. **Repeat**
 4. **Merge** the two closest clusters
 5. **Update** the proximity matrix
 6. **Until** only a single cluster remains
- Key operation is the computation of the **proximity of two clusters**
 - Different approaches to defining the **distance between clusters** distinguish the different algorithms

Starting Situation

- Start with **single-point clusters** and a proximity matrix **between points**



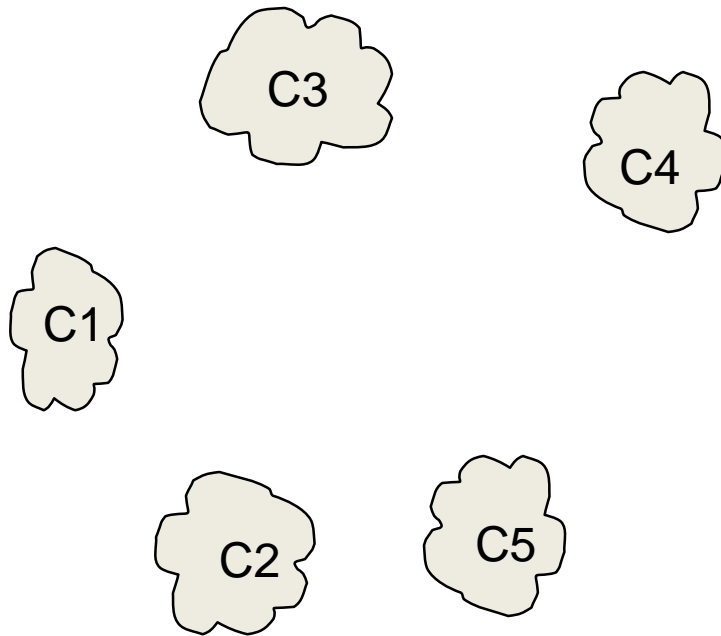
| | p1 | p2 | p3 | p4 | p5 | ... |
|----|----|----|----|----|----|-----|
| p1 | | | | | | |
| p2 | | | | | | |
| p3 | | | | | | |
| p4 | | | | | | |
| p5 | | | | | | |
| . | | | | | | |
| . | | | | | | |
| . | | | | | | |

Proximity Matrix



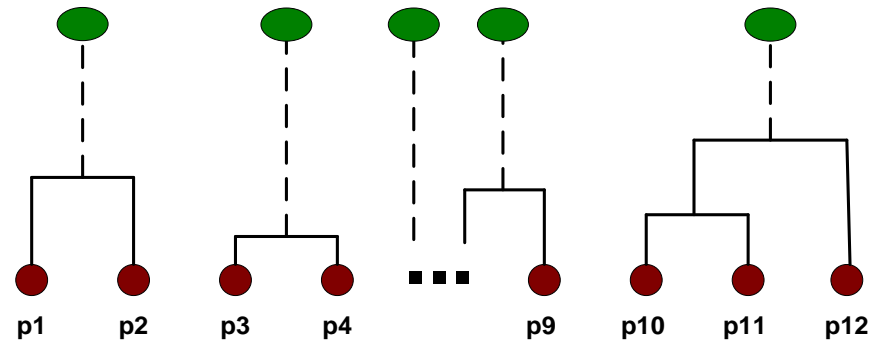
Intermediate Situation

- After some merging steps, we have some clusters and a proximity matrix **between clusters**



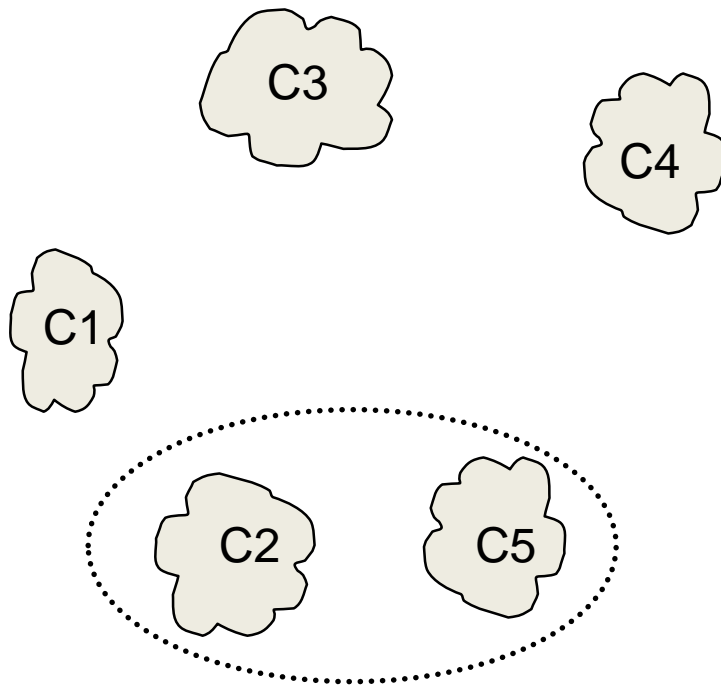
| | C1 | C2 | C3 | C4 | C5 |
|----|----|----|----|----|----|
| C1 | | | | | |
| C2 | | | | | |
| C3 | | | | | |
| C4 | | | | | |
| C5 | | | | | |

Proximity Matrix



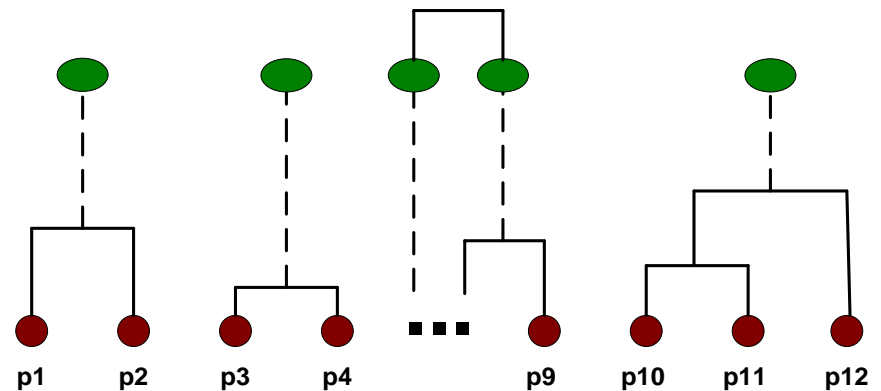
Intermediate Situation

- We want to merge the two closest clusters (C2 and C5) and update the proximity matrix.



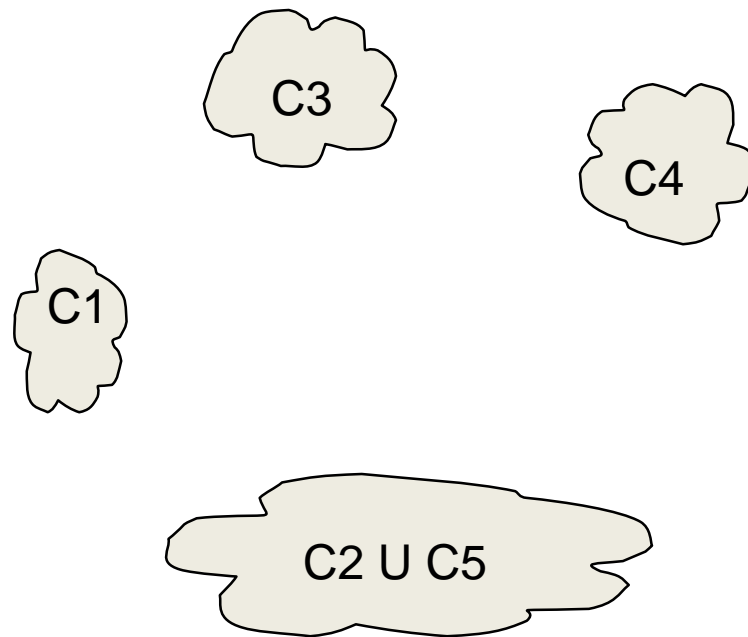
| | C1 | C2 | C3 | C4 | C5 |
|----|----|----|----|----|----|
| C1 | | | | | |
| C2 | | | | | |
| C3 | | | | | |
| C4 | | | | | |
| C5 | | | | | |

Proximity Matrix



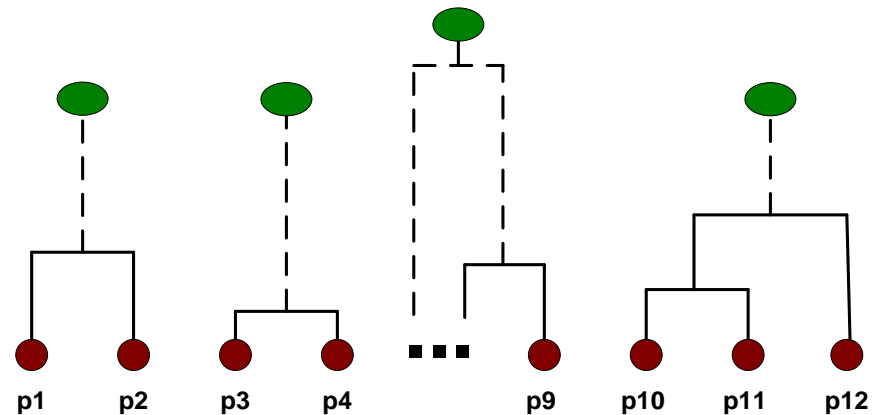
After Merging

- The question is “How do we update the proximity matrix?”

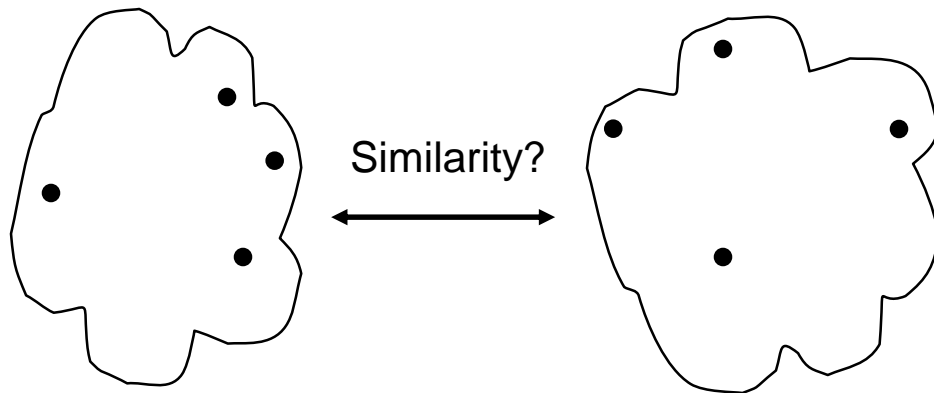


| | C1 | C2 U C5 | C3 | C4 |
|---------|----|---------------|----|----|
| C1 | | ? | | |
| C2 U C5 | ? | ? | ? | ? |
| C3 | | ? | | |
| C4 | | ? | | |

Proximity Matrix



How to Define Inter-Cluster Similarity

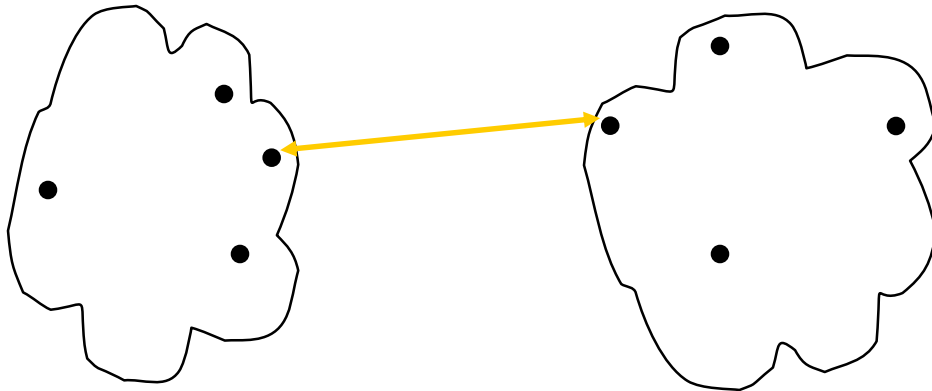


- MIN
- MAX
- Group Average
- Distance Between Centroids
- Other methods driven by an objective function
 - Ward's Method uses squared error

| | p1 | p2 | p3 | p4 | p5 | ... |
|----|----|----|----|----|----|-----|
| p1 | | | | | | |
| p2 | | | | | | |
| p3 | | | | | | |
| p4 | | | | | | |
| p5 | | | | | | |
| . | | | | | | |
| . | | | | | | |
| . | | | | | | |

Proximity Matrix

How to Define Inter-Cluster Similarity

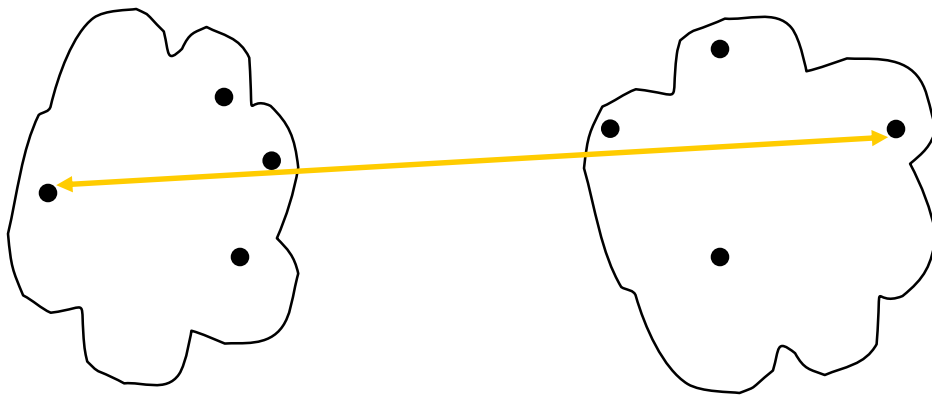


- **MIN**
- **MAX**
- **Group Average**
- **Distance Between Centroids**
- **Other methods driven by an objective function**
 - Ward's Method uses squared error

| | p1 | p2 | p3 | p4 | p5 | ... |
|----|----|----|----|----|----|-----|
| p1 | | | | | | |
| p2 | | | | | | |
| p3 | | | | | | |
| p4 | | | | | | |
| p5 | | | | | | |
| . | | | | | | |
| . | | | | | | |
| . | | | | | | |

Proximity Matrix

How to Define Inter-Cluster Similarity

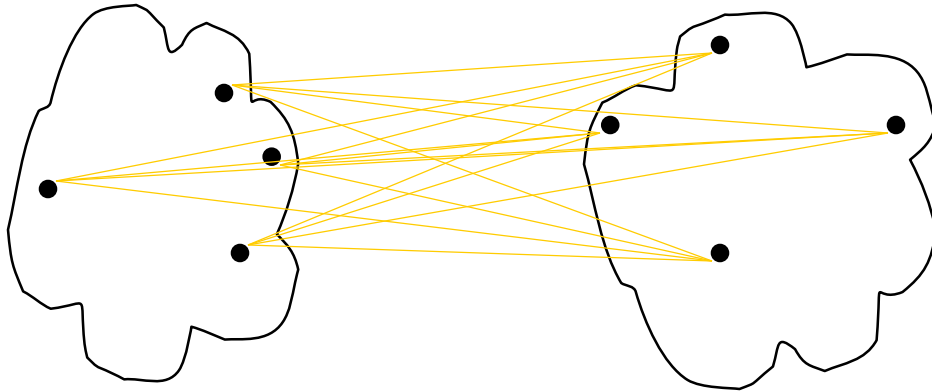


- MIN
- MAX
- Group Average
- Distance Between Centroids
- Other methods driven by an objective function
 - Ward's Method uses squared error

| | p1 | p2 | p3 | p4 | p5 | ... |
|----|----|----|----|----|----|-----|
| p1 | | | | | | |
| p2 | | | | | | |
| p3 | | | | | | |
| p4 | | | | | | |
| p5 | | | | | | |
| . | | | | | | |
| . | | | | | | |
| . | | | | | | |

Proximity Matrix

How to Define Inter-Cluster Similarity

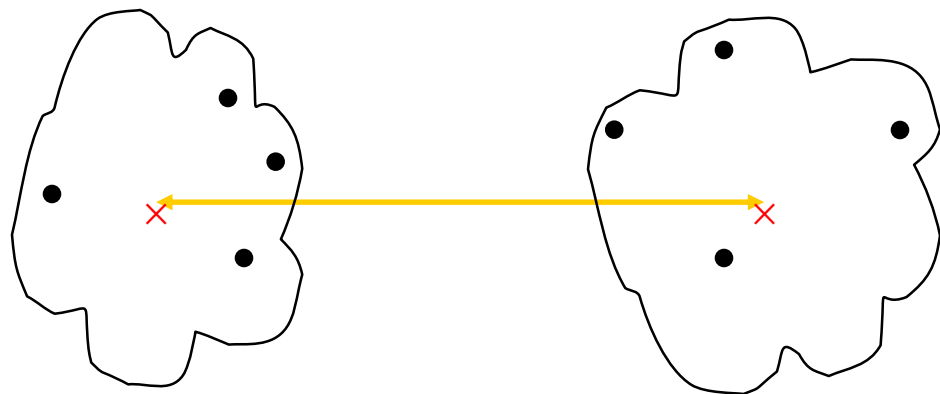


- MIN
- MAX
- **Group Average**
- Distance Between Centroids
- Other methods driven by an objective function
 - Ward's Method uses squared error

| | p1 | p2 | p3 | p4 | p5 | ... |
|----|----|----|----|----|----|-----|
| p1 | | | | | | |
| p2 | | | | | | |
| p3 | | | | | | |
| p4 | | | | | | |
| p5 | | | | | | |
| . | | | | | | |
| . | | | | | | |
| . | | | | | | |

Proximity Matrix

How to Define Inter-Cluster Similarity



- MIN
- MAX
- Group Average
- **Distance Between Centroids**
- Other methods driven by an objective function
 - Ward's Method uses squared error

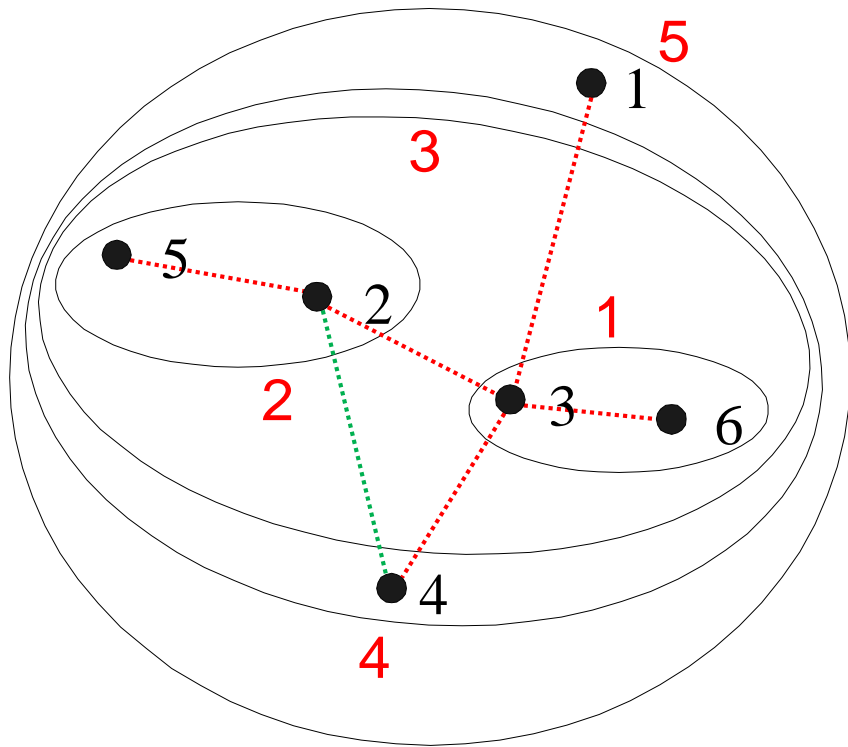
| | p1 | p2 | p3 | p4 | p5 | ... |
|----|----|----|----|----|----|-----|
| p1 | | | | | | |
| p2 | | | | | | |
| p3 | | | | | | |
| p4 | | | | | | |
| p5 | | | | | | |
| . | | | | | | |
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| . | | | | | | |

Proximity Matrix

Single Link – Complete Link

- Another way to view the processing of the hierarchical algorithm is that we create links between the **elements** in order of **increasing distance**
 - The MIN – **Single Link**, will merge two clusters when a **single pair** of elements is linked
 - The MAX – **Complete Linkage** will merge two clusters when **all pairs** of elements have been linked.

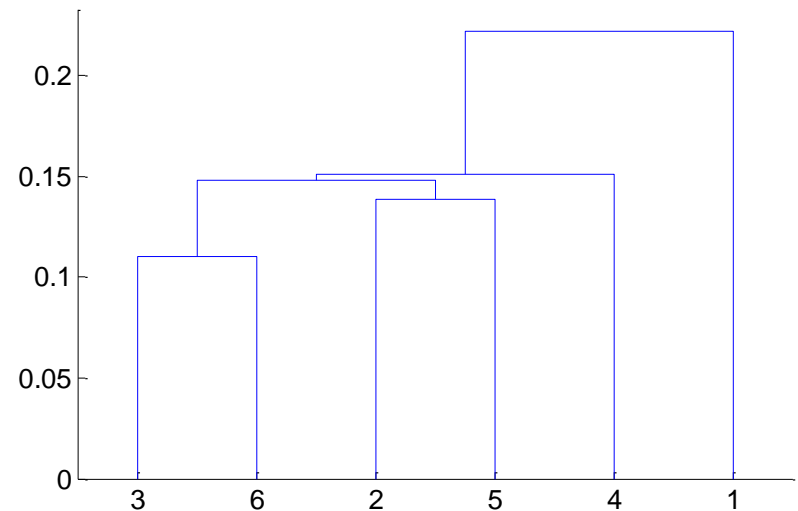
Hierarchical Clustering: MIN



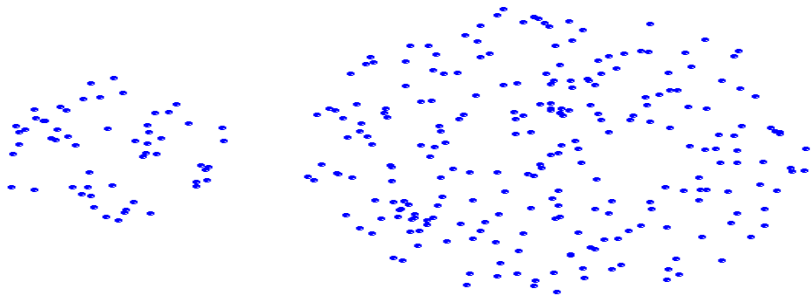
Nested Clusters

| | 1 | 2 | 3 | 4 | 5 | 6 |
|---|------------|------------|------------|------------|------------|------------|
| 1 | 0 | .24 | .22 | .37 | .34 | .23 |
| 2 | .24 | 0 | .15 | .20 | .14 | .25 |
| 3 | .22 | .15 | 0 | .15 | .28 | .11 |
| 4 | .37 | .20 | .15 | 0 | .29 | .22 |
| 5 | .34 | .14 | .28 | .29 | 0 | .39 |
| 6 | .23 | .25 | .11 | .22 | .39 | 0 |

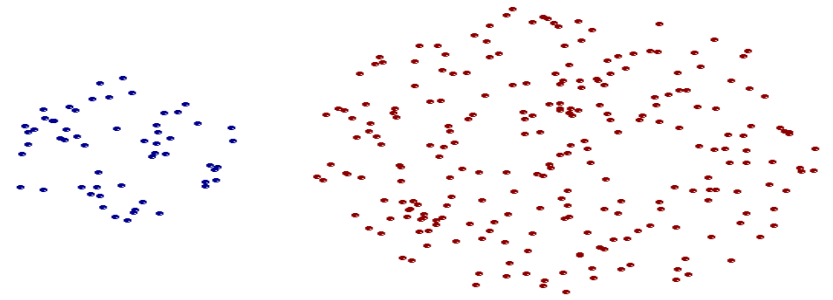
Dendrogram



Strength of MIN



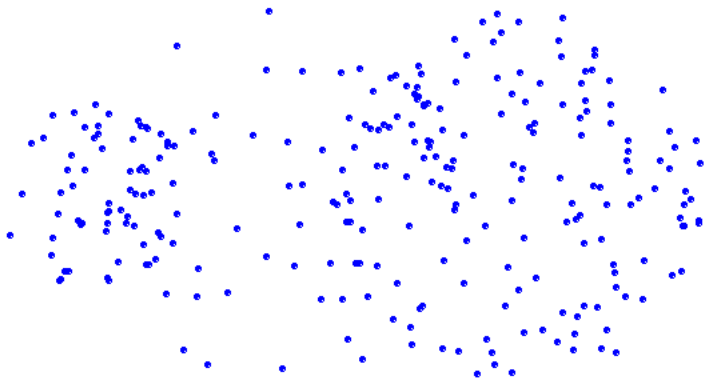
Original Points



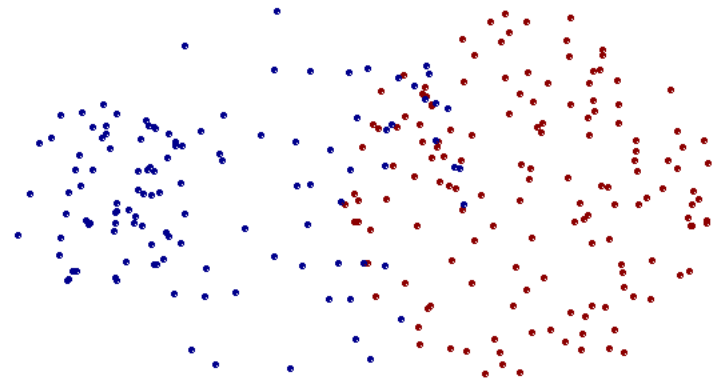
Two Clusters

- Can handle non-elliptical shapes

Limitations of MIN



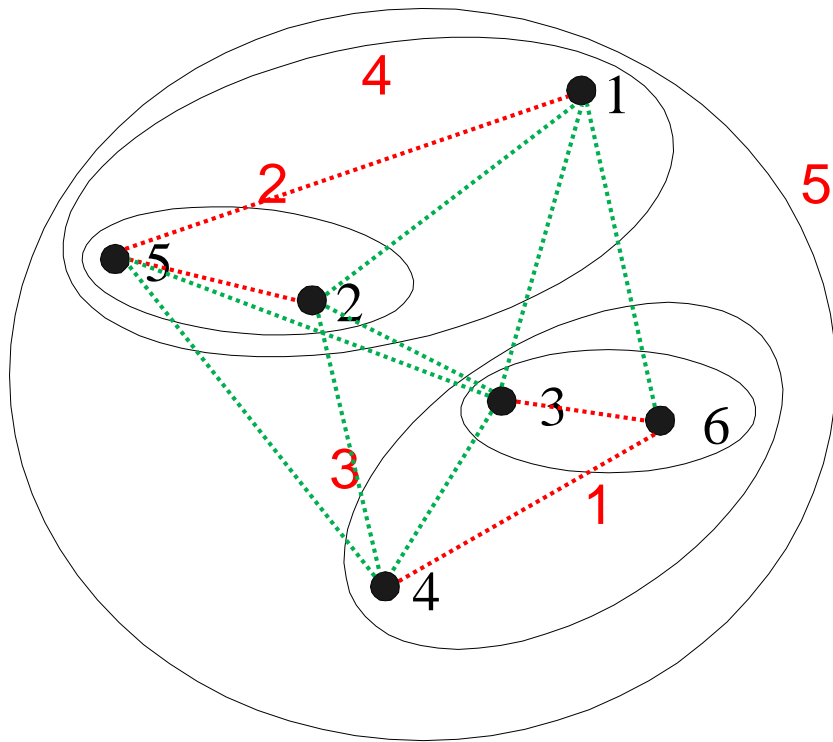
Original Points



Two Clusters

- Sensitive to noise and outliers

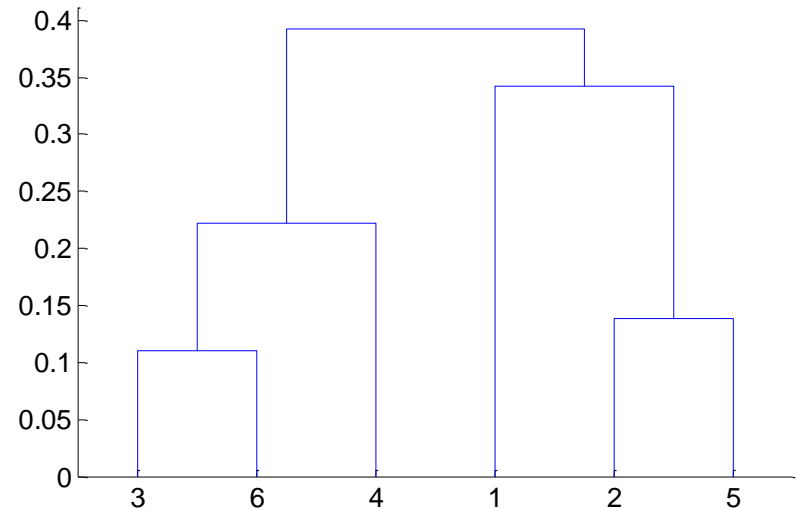
Hierarchical Clustering: MAX



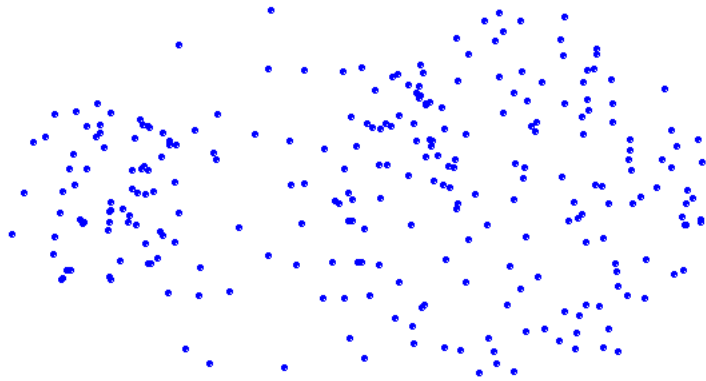
Nested Clusters

Dendrogram

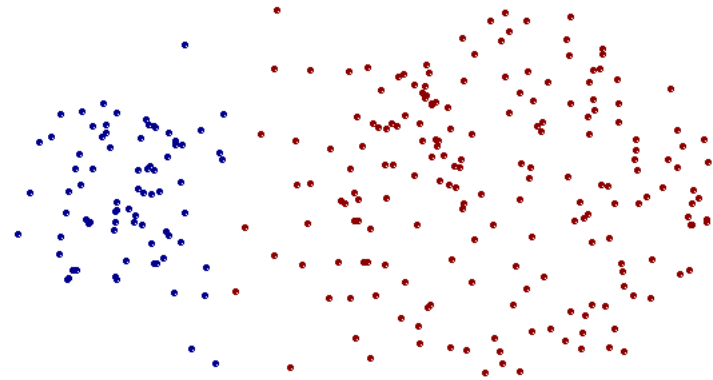
| | 1 | 2 | 3 | 4 | 5 | 6 |
|---|-----|-----|-----|-----|-----|-----|
| 1 | 0 | .24 | .22 | .37 | .34 | .23 |
| 2 | .24 | 0 | .15 | .20 | .14 | .25 |
| 3 | .22 | .15 | 0 | .15 | .28 | .11 |
| 4 | .37 | .20 | .15 | 0 | .29 | .22 |
| 5 | .34 | .14 | .28 | .29 | 0 | .39 |
| 6 | .23 | .25 | .11 | .22 | .39 | 0 |



Strength of MAX



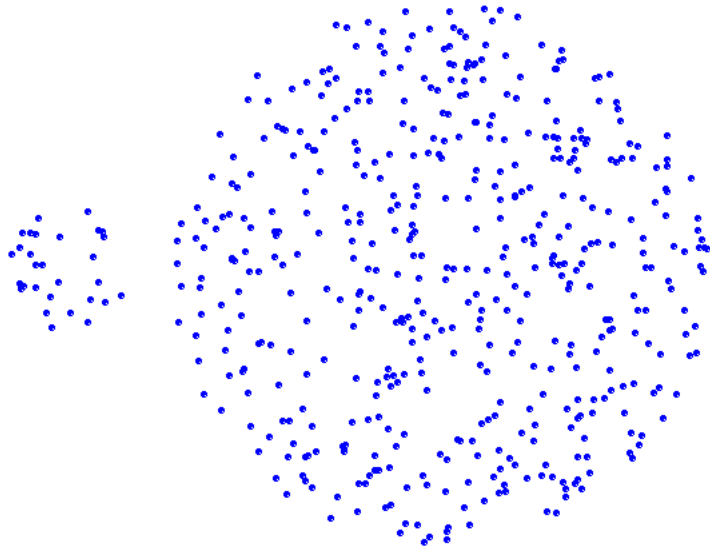
Original Points



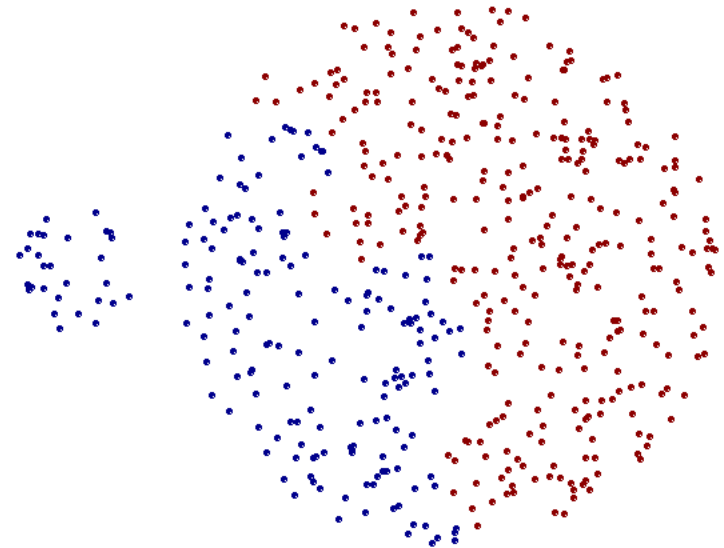
Two Clusters

- Less susceptible to noise and outliers

Limitations of MAX



Original Points



Two Clusters

- Tends to break large clusters
- Biased towards globular clusters

Cluster Similarity: Group Average

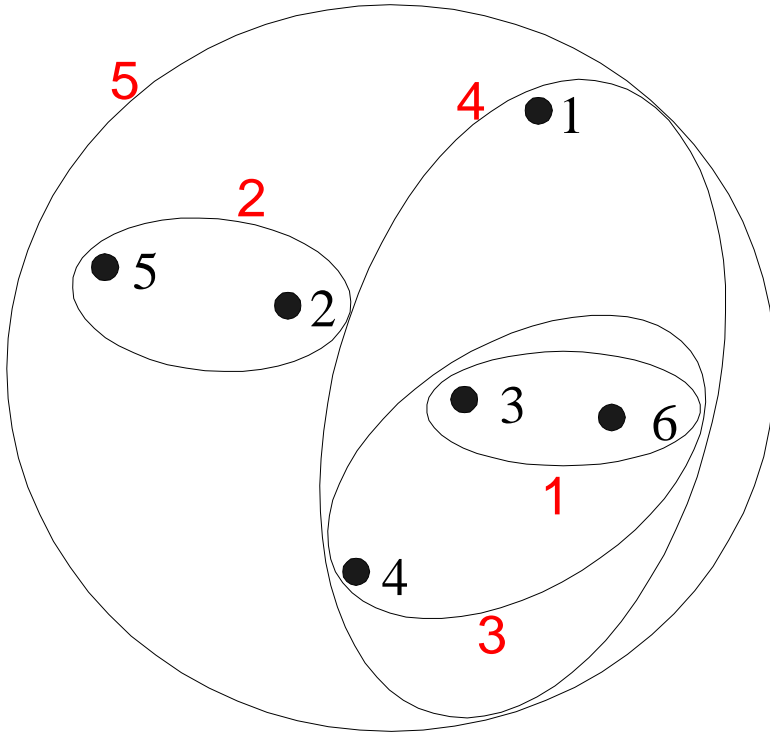
- Proximity of two clusters is the average of pairwise proximity between points in the two clusters.

$$\text{proximity}(\text{Cluster}_i, \text{Cluster}_j) = \frac{\sum_{\substack{p_i \in \text{Cluster}_i \\ p_j \in \text{Cluster}_j}} \text{proximity}(p_i, p_j)}{|\text{Cluster}_i| * |\text{Cluster}_j|}$$

- Need to use average connectivity for scalability since total proximity favors large clusters

| | 1 | 2 | 3 | 4 | 5 | 6 |
|---|-----|-----|-----|-----|-----|-----|
| 1 | 0 | .24 | .22 | .37 | .34 | .23 |
| 2 | .24 | 0 | .15 | .20 | .14 | .25 |
| 3 | .22 | .15 | 0 | .15 | .28 | .11 |
| 4 | .37 | .20 | .15 | 0 | .29 | .22 |
| 5 | .34 | .14 | .28 | .29 | 0 | .39 |
| 6 | .23 | .25 | .11 | .22 | .39 | 0 |

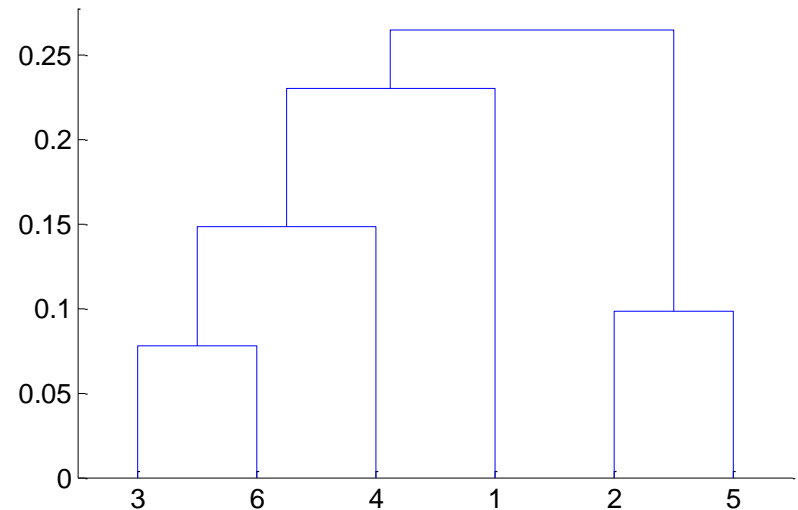
Hierarchical Clustering: Group Average



Nested Clusters

Dendrogram

| | 1 | 2 | 3 | 4 | 5 | 6 |
|---|-----|-----|-----|-----|-----|-----|
| 1 | 0 | .24 | .22 | .37 | .34 | .23 |
| 2 | .24 | 0 | .15 | .20 | .14 | .25 |
| 3 | .22 | .15 | 0 | .15 | .28 | .11 |
| 4 | .37 | .20 | .15 | 0 | .29 | .22 |
| 5 | .34 | .14 | .28 | .29 | 0 | .39 |
| 6 | .23 | .25 | .11 | .22 | .39 | 0 |



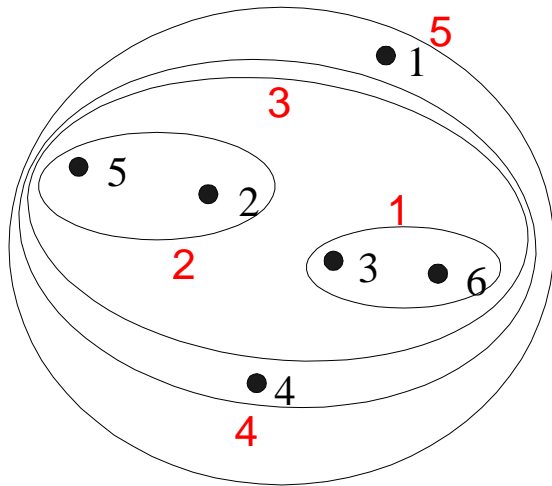
Hierarchical Clustering: Group Average

- Compromise between Single and Complete Link
- Strengths
 - Less susceptible to noise and outliers
- Limitations
 - Biased towards globular clusters

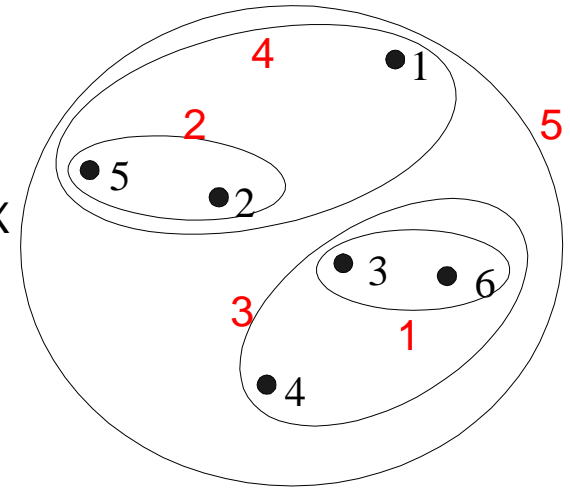
Cluster Similarity: Ward's Method

- Similarity of two clusters is based on the **increase** in **squared error (SSE)** when two clusters are merged
 - Similar to group average if distance between points is sum of squares distance
- Less susceptible to noise and outliers
- Biased towards globular clusters
- Hierarchical analogue of K-means
 - Can be used to initialize K-means

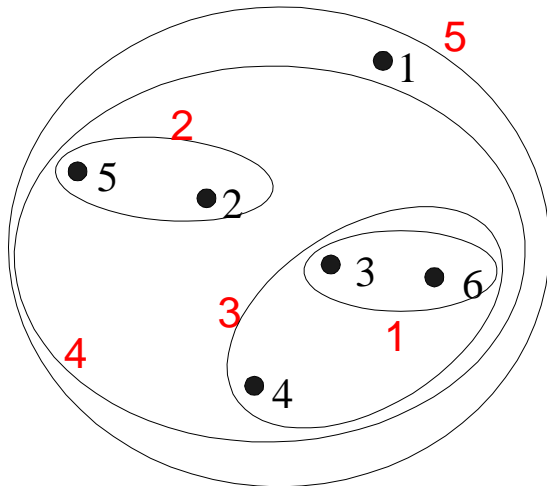
Hierarchical Clustering: Comparison



MIN

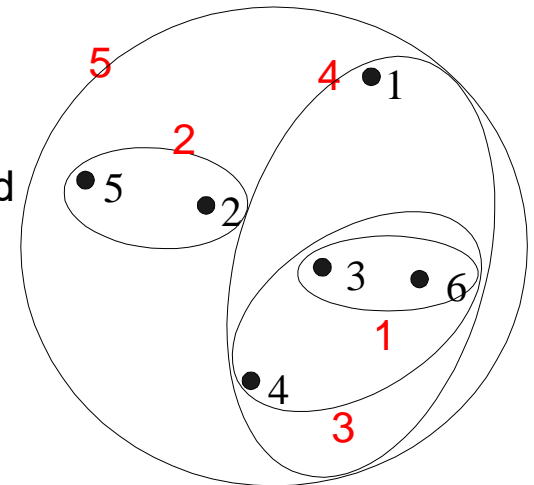


MAX



Group Average

Ward's Method



Hierarchical Clustering: Time and Space requirements

- $O(N^2)$ space since it uses the proximity matrix.
 - N is the number of points.
- $O(N^3)$ time in many cases
 - There are N steps and at each step the size, N^2 , proximity matrix must be updated and searched
 - Complexity can be reduced to $O(N^2 \log(N))$ time for some approaches

Hierarchical Clustering: Problems and Limitations

- Computational complexity in time and space
- Once a decision is made to combine two clusters, it cannot be undone
- No objective function is directly minimized
- Different schemes have problems with one or more of the following:
 - Sensitivity to noise and outliers
 - Difficulty handling different sized clusters and convex shapes
 - Breaking large clusters

DBSCAN

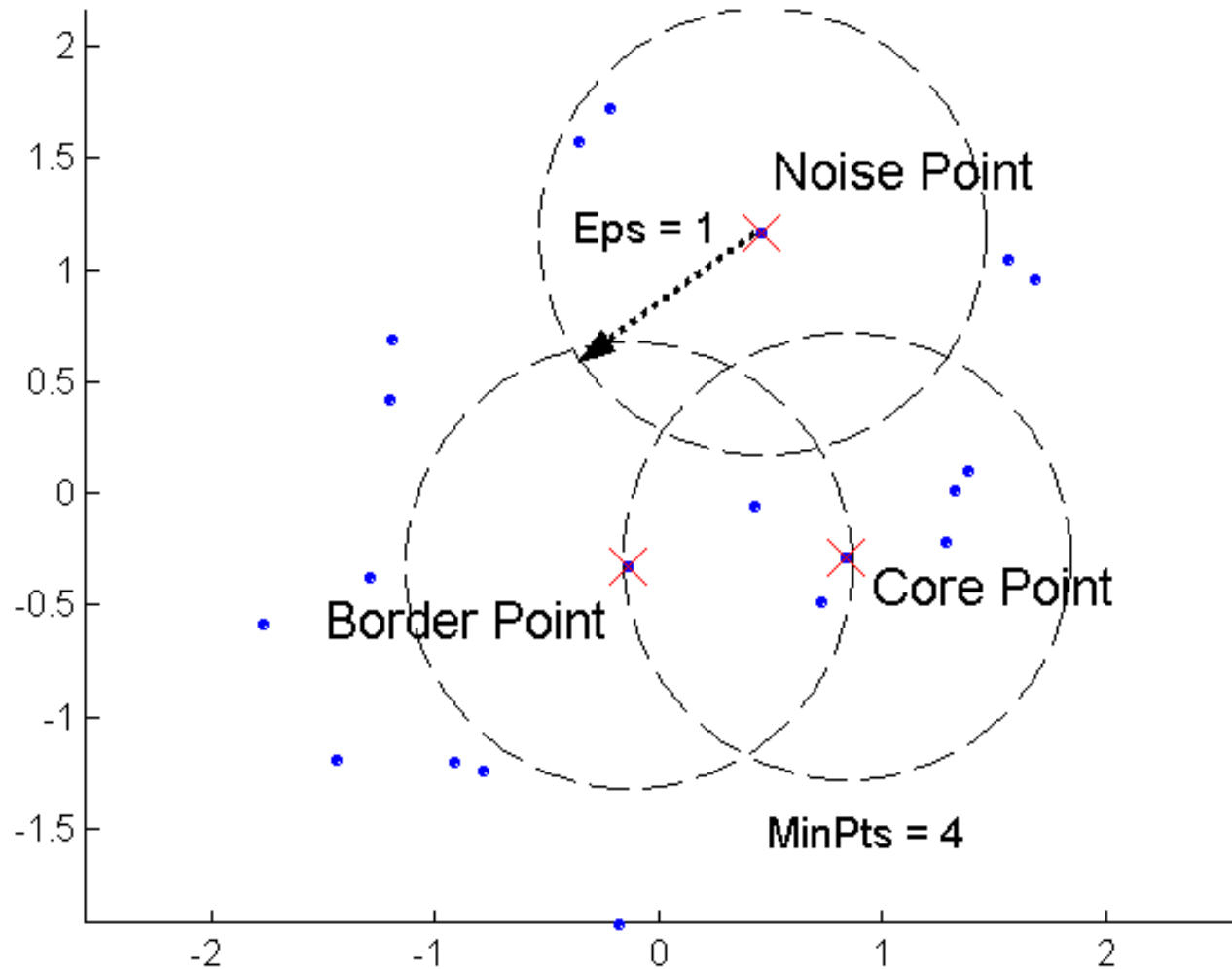
DBSCAN: Density-Based Clustering

- **DBSCAN** is a **Density-Based Clustering** algorithm
- **Reminder:** In density based clustering we partition points into dense regions separated by not-so-dense regions.
- **Important Questions:**
 - How do we measure density?
 - What is a dense region?
- **DBSCAN:**
 - **Density at point p :** number of points within a circle of radius **Eps**
 - **Dense Region:** A circle of radius **Eps** that contains at least **MinPts** points

DBSCAN

- Characterization of points
 - A point is a **core point** if it has more than a specified number of points (**MinPts**) within **Eps**
 - These points belong in a **dense region** and are at the **interior** of a cluster
 - A **border point** has fewer than **MinPts** within **Eps**, but is in the neighborhood of a **core** point.
 - A **noise point** is any point that is not a core point or a border point.

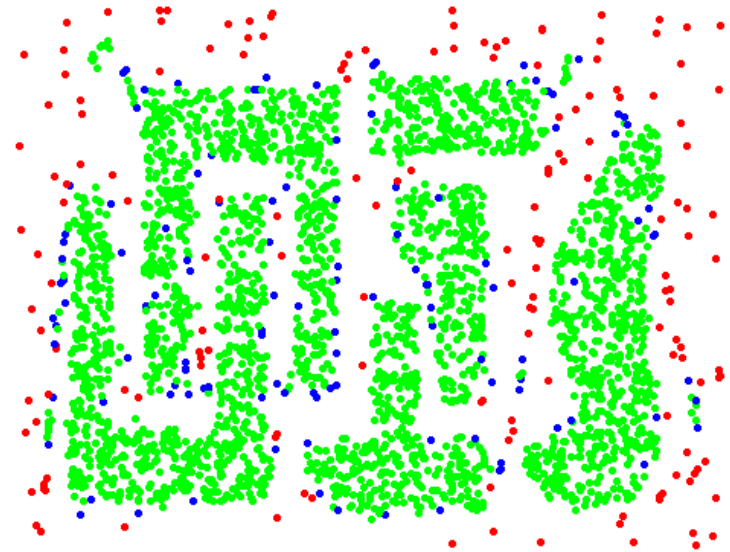
DBSCAN: Core, Border, and Noise Points



DBSCAN: Core, Border and Noise Points



Original Points

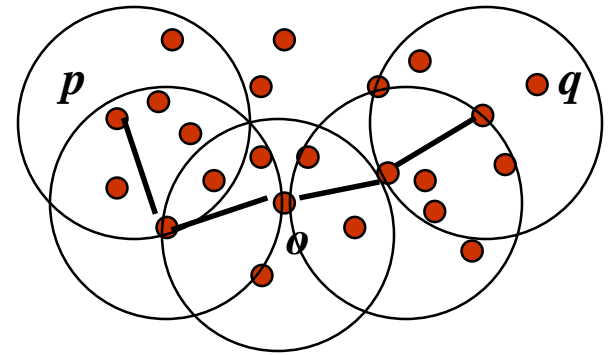
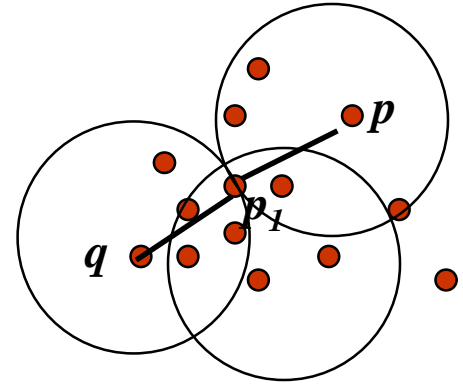


Point types: core,
border and noise

Eps = 10, MinPts = 4

Density-Connected points

- **Density edge**
 - We place an **edge** between two core points **q** and **p** if they are within distance **Eps**.
- **Density-connected**
 - A point **p** is **density-connected** to a point **q** if there is a **path of edges** from **p** to **q**

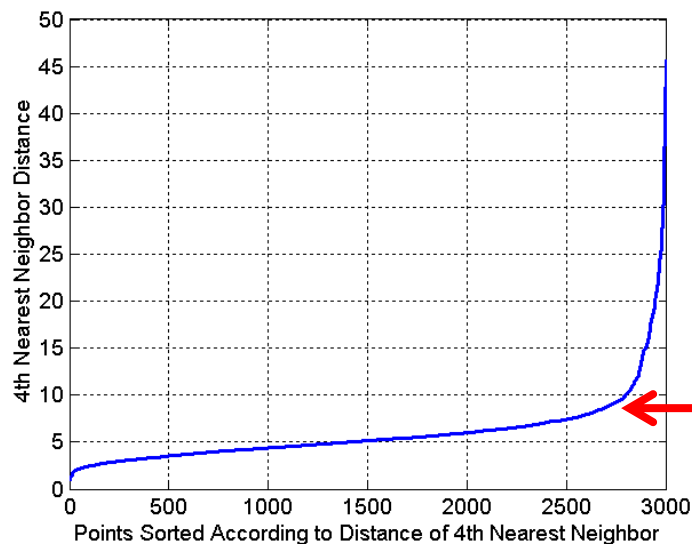


DBSCAN Algorithm

- Label points as **core**, **border** and **noise**
- Eliminate **noise** points
- For every **core** point p that has not been assigned to a cluster
 - Create a new cluster with the point p and all the points that are **density-connected** to p .
- Assign **border** points to the cluster of the closest core point.

DBSCAN: Determining Eps and MinPts

- Idea is that for points in a cluster, their k^{th} nearest neighbors are at roughly the same distance
- Noise points have the k^{th} nearest neighbor at farther distance
- So, plot sorted distance of every point to its k^{th} nearest neighbor
- Find the distance d where there is a “knee” in the curve
 - $\text{Eps} = d$, $\text{MinPts} = k$

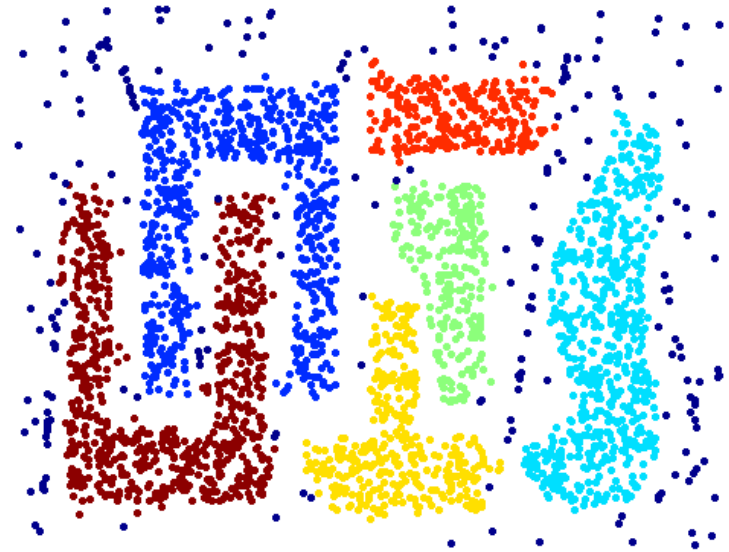


Eps ~ 7-10
MinPts = 4

When DBSCAN Works Well



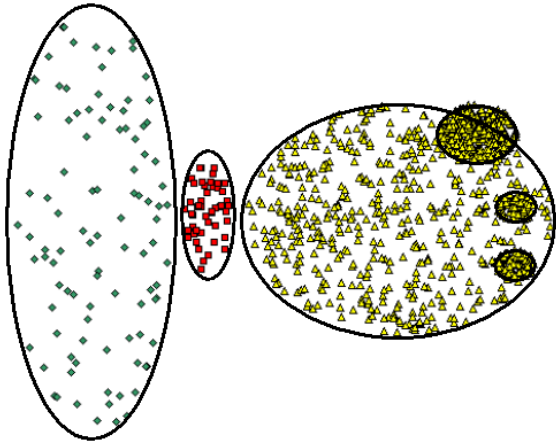
Original Points



Clusters

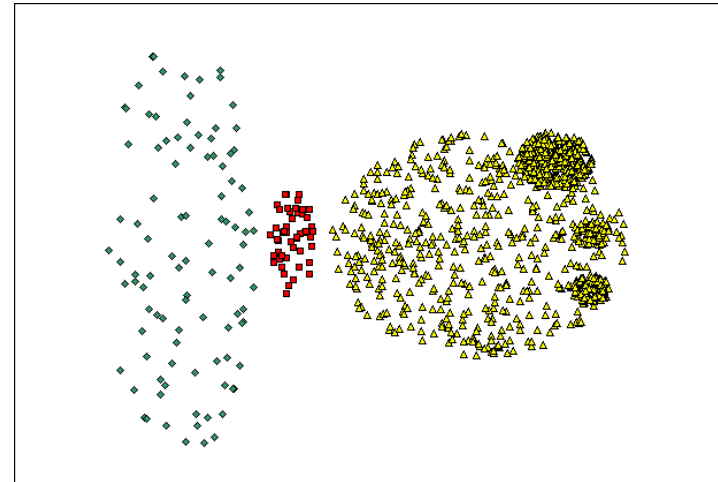
- Resistant to Noise
- Can handle clusters of different shapes and sizes

When DBSCAN Does NOT Work Well

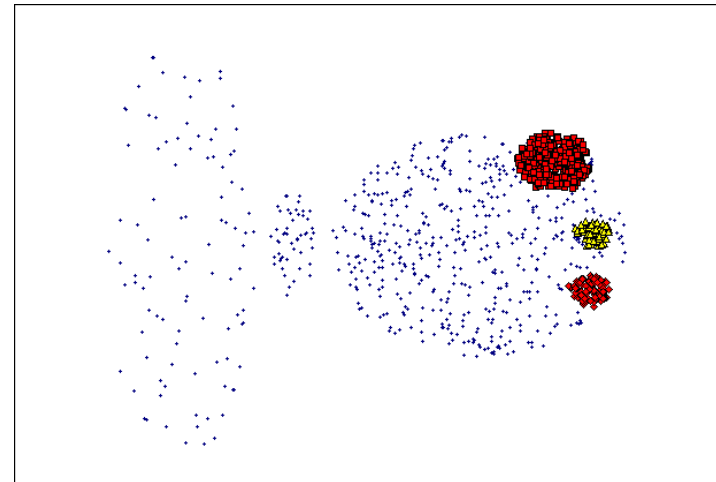


Original Points

- Varying densities
- High-dimensional data



(MinPts=4, Eps=9.75).



(MinPts=4, Eps=9.92)

DBSCAN: Sensitive to Parameters

Figure 8. DBScan results for DS1 with MinPts at 4 and Eps at (a) 0.5 and (b) 0.4.

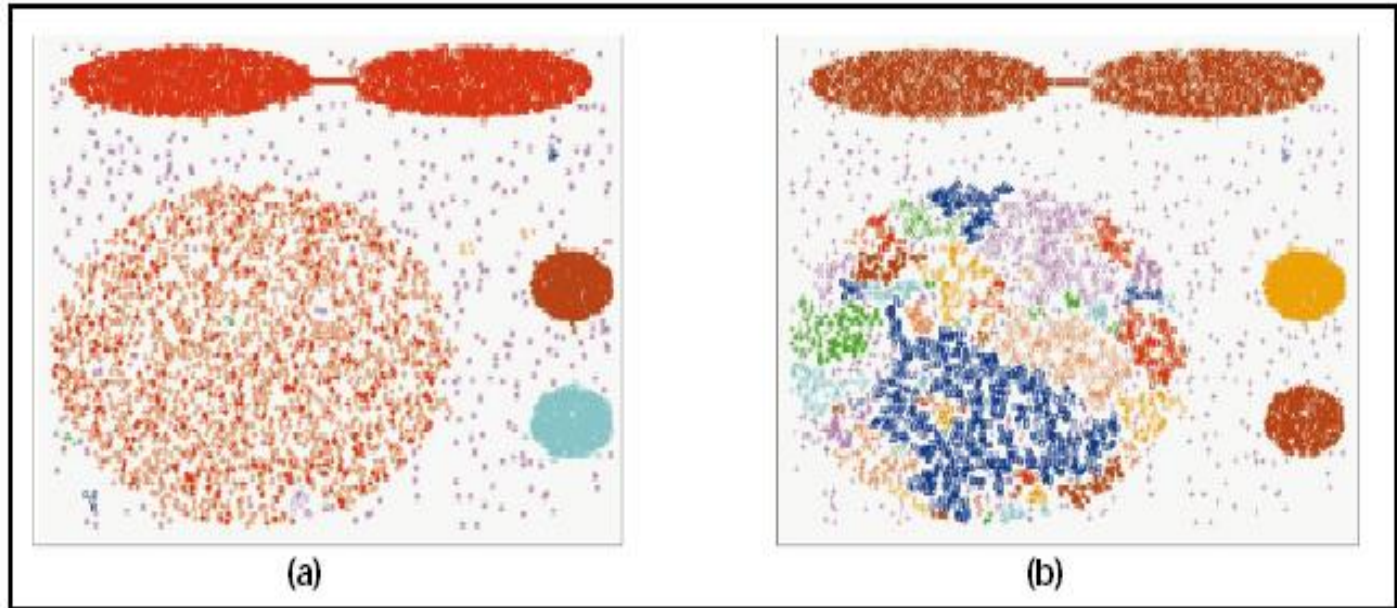
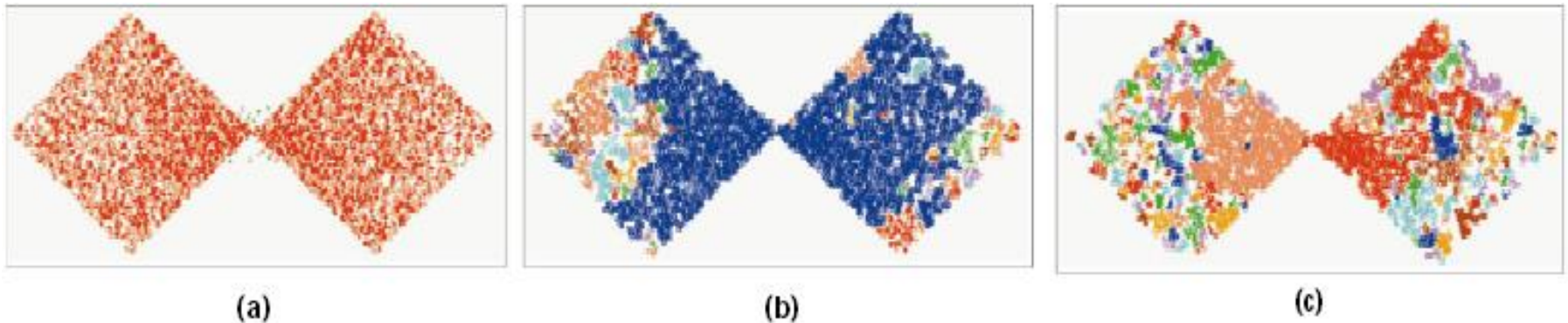


Figure 9. DBScan results for DS2 with MinPts at 4 and Eps at (a) 5.0, (b) 3.5, and (c) 3.0.



Other algorithms

- **PAM, CLARANS**: Solutions for the **k-medoids** problem
- **BIRCH**: Constructs a **hierarchical tree** that acts a summary of the data, and then clusters the leaves.
- **MST**: Clustering using the **Minimum Spanning Tree**.
- **ROCK**: clustering **categorical data** by neighbor and link analysis
- **LIMBO, COOLCAT**: Clustering **categorical data** using **information theoretic** tools.
- **CURE**: **Hierarchical** algorithm uses different representation of the cluster
- **CHAMELEON**: **Hierarchical** algorithm uses **closeness and interconnectivity** for merging