# Trading Privacy for Information Loss in the Blink of an Eye 

A. Pilalidou *<br>FMT Worldwide<br>Limassol, Cyprus

Dept. of Computer Science,
Univ. Ioannina, Hellas

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Univ. of Ioannina

## Summary

- Private data publishing involves hiding the relationship of a person with sensitive data for this person (typically via noise injection, or via hiding a person's info in a crowd of similar tuples). SoA suggests that a data curator anonymizes data off-line, by trying to maximize the value of a utility function. What if we refute this assumption?
- In this paper, we provide a method that allows the curator to negotiate information loss to privacy. We want to allow the curator to explore different alternatives in an attempt to reach an equilibrium on the tradeoff of privacy relaxation vs. info loss (either via deleting outlier tuples or via abstracting more)
- To support this interaction, we (have to) provide :
- Instant answers
- Recommendations on alternatives
- Intuition on decisions

| Name | Age | Work_class | Education | Hours/week |
| :---: | :---: | :---: | :---: | :---: |
| Thales | 39 | Private | Hs-grad | 40 |
| Anaximander | 38 | Private | Hs-grad | 50 |
| Anaximenes | 37 | Private | Hs-grad | 40 |
| Pythagoras | 38 | Private | 11th | 45 |
| Gorgias | 28 | Loc-gov | Bachelors | 30 |
| Heraclitus | 31 | Federal-gov | Master | 50 |
| Empedocles | 30 | State-gov | Bachelors | 60 |
| Leucippus | 32 | Self-emp-not-inc | Bachelors | 50 |
| Democritus | 35 | Self-emp-inc | Prof-school | 54 |
| Protagoras | 33 | Self-emp-inc | Assoc-acd | 40 |

## $k$-anonymity

A relation $T$ is $\boldsymbol{k}$-anonymous when every tuple of the relation is identical to k -1 other tuples with respect to their Quasi-Identifier set of attributes.

| Name |
| :---: |
| Thales |
| Anaximander |
| Anaximenes |
| Pythagoras |
| Gorgias |
| Heraclitus |
| Empedocles |
| Leurippus |
| Democritus |
| Protagoras |


| Age | Work_class | Education | Hours/week |
| :---: | :---: | :---: | :---: |
| $37-41$ | Private | Without-post-secondary | 40 |
| $37-41$ | Private | Without-post-secondary | 50 |
| $37-41$ | Private | Without-post-secondary | 40 |
| $37-41$ | Private | Without-post-secondary | 45 |
| $27-31$ | Gov | Post-secondary | 30 |
| $27-31$ | Gov | Post-secondary | 50 |
| $27-31$ | Gov | Post-secondary | 60 |
| $32-36$ | Self-emp | Post-secondary | 50 |
| $32-36$ | Selfemp | Post-secondary | 54 |
| $32-36$ | Self-emp | Post-secondary | 40 |



## State-of-the-art

- All the related bibliography is based on the assumption that we have plenty of off-line time to process the data set
- The emphasis has been placed
- To different privacy criteria and the corresponding attacks they prevent
- To fast algorithms for exact solutions to the problem of optimal anonymization (wrt to a utility function)
- Still: not fast enough for user-time (in the order of minutes / hours / ...)


## Research questions

- Can we help the data curator negotiate different configurations of privacy, generalization and suppression and decide what is best without resorting to some non-intuitive utility function?
- e.g., by paying the price for less privacy (lower k) to attain a better value of suppression (less removed tuples) and, thus, higher information utility?
- Can the system guide the search by suggesting alternatives - esp., when tested configurations are impossible to attain?
- Can we do it in user time (i.e., without delays noticeable by the user)?


## Our method

- We pre-compute, off-line
- All the possible combinations of levels for the QI attributes - organized in a lattice of anonymization schemes
- The suppression histogram of each such combination (for a specific privacy criterion) - i.e., for every combination we know the amount of tuples that have to be suppressed for a specific value of the privacy criterion
- The user specifies a request with 3 parameters as constraints (max height per hierarchy, max tolerable suppression, min tolerable $k$ or $/$ ).
- If a solution for this value combination exists
- Among all the solutions that satisfy the request, we present the solution that is located at the lowest generalization height
- If no such solution exists
- we provide the user with 3 suggestions (i.e., approximate answers ), each relaxing one of the 3 abovementioned constraints



## The anonymization lattice

Here, Ql=3 (Age, Workclass, Education, each with its own hierarchy)

A node is annotated by the levels of its Q attributes

Eg. 302 means
L3 for age
LO for workclass
L2 for education

## Histograms




- Histograms allow us to compute the amount of suppression for a given value of $k$ (equiv. I).
- E.g., to achieve 3-anonymity in level A1W1R1 we must suppress groups with size 1 or 2 => 17 tuples
(17=1*11+2*3). $1580(1 * 834+2 * 373)$.


This is the lattice for QI=3 annotated with the number of suppressed tuples for k=3


Assume the user requests:
h = 121
K = 3
MaxSupp = 20

Observe vmax 121


Assume the user requests:
h = 121
K = 3
MaxSupp = 20

The exact solution is 111 with \#supp. $=17$


Assume the user
requests:
h = 121
K = 3
MaxSupp = 8

Observe vmax 121: it fails to meet all three constraints


Assume the user requests:
h = 121
K = 3
MaxSupp = 8

## Suggestions:

## Closest k:

Node 121, k=2

Closest height:
Node 400, h=4

Closest maxSupp:
Node 121, maxsupp=11

## Aigorithn at a gidnce

## Input:

- Input relation R + hierarchies H + lattice with histograms
- A user request (k, h, maxSupp) with the user constraints

1. Identify top-acceptable node $v_{\max }$
2. If $v_{\max }$ answers the ( $k, h$, maxSupp)

- Search within the sublattice of vmax for the lowest possible node that also answers ( $k$, h, maxSupp)

3. Else

- Relax MaxSupp: stay at $\mathrm{v}_{\text {max }}$ (respect $\mathbf{h}$ ) and find the suppression value for k (respect k)
- Relax $k$ : stay at $\mathrm{v}_{\max }($ respect $\mathbf{h})$ and find the largest $k$ that suppresses less than maxSupp (respect maxSupp)
- Relax h (retain k, maxSupp) and answer outside the sublattice:
- Binary search between $v_{\text {max }}$ and lattice's top
- Exhaust all nodes of a level: if nobody answers, binary search between top and this level; else, whenever a node answers, perform binary downwards
- Stop when it is impossible to descend and the last level is exhaustively tested


## Some experimental results





h




MaxSupp





Number of visited nodes for different QI, k, h, MaxSupp. All times range between 1 and 8 msec. Light coloring is for exact matches and dark coloring is for approximate matches

## Histogram construction time



K-anonymity


Naïve I-diversity

- Clearly dependent upon QI size, with an exponential tendency
- Remember that this is a compute-once use-many situation


## 

- Can we respond in user time to anonymization requests? Can we suggest anonymization schemes that are approximately close to the original user request?
- Yes to both! We have two ways to address the above, depending on the price we are willing to pay wrt the offline preprocessing of the lattice
- Full lattice (preprocessing \& query answering)
- Exact answers and suggestions in less than 10 msec (depends upon lattice size)
- $18 \mathrm{sec}-20 \mathrm{~min}$ preprocessing time (depending on both the QI and the data size)
- The long $v$. of the paper (also long $v$ of the talk) contains:
- Theoretical guarantees that our method is guaranteed to provide the best possible answers for the given user requests.
- Extensive discussion on the validity of the problem. To the best of our knowledge, this the first systematic study on the interdependency of suppression, generalization and privacy in a quantitative fashion.
- Extensive experimental results, over the IPUMS and the Adult data set.
- Partial lattice: o handle the issue of scale (as the off-line lattice-and-histogram construction is dominated by both the Ql size and the data size) we provide a method for the selection of a small subset of characteristic nodes of the lattice to be annotated with histograms, based on a small number of tests that rank Ql levels for the grouping power.



[^0]:    *work conducted in
    Univ. Ioannina

