Digital Image Processing

Intensity Transformations
(Point Processing)

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“It makes all the difference whether one sees darkness through the light or brightness through the shadows”

David Lindsay
(Scottish Novelist)
Over the next few lectures we will look at image enhancement techniques working in the spatial domain:

- What is image enhancement?
- Different kinds of image enhancement
- Point processing
- Histogram processing
- Spatial filtering
What Is Image Enhancement?

Image enhancement is the process of making images more useful.

The reasons for doing this include:

- Highlighting interesting detail in images
- Removing noise from images
- Making images more visually appealing
Image Enhancement Examples

Image Enhancement Examples (cont…)

Image Enhancement Examples (cont...)

Image Enhancement Examples (cont...)

There are two broad categories of image enhancement techniques

- Spatial domain techniques
  - Direct manipulation of image pixels
- Frequency domain techniques
  - Manipulation of Fourier transform or wavelet transform of an image

For the moment we will concentrate on techniques that operate in the spatial domain.
In this lecture we will look at image enhancement point processing techniques:

- What is point processing?
- Negative images
- Thresholding
- Logarithmic transformation
- Power law transforms
- Grey level slicing
- Bit plane slicing
A Note About Grey Levels

So far when we have spoken about image grey level values we have said they are in the range $[0, 255]$

- Where 0 is black and 255 is white

There is no reason why we have to use this range

- The range $[0, 255]$ stems from display technologies

For many of the image processing operations in this lecture grey levels are assumed to be given in the range $[0.0, 1.0]$
Most spatial domain enhancement operations can be reduced to the form

\[ g(x, y) = T[f(x, y)] \]

where \( f(x, y) \) is the input image, \( g(x, y) \) is the processed image and \( T \) is some operator defined over some neighbourhood of \( (x, y) \).
The simplest spatial domain operations occur when the neighbourhood is simply the pixel itself.

In this case, $T$ is referred to as a grey level transformation function or a point processing operation.

Point processing operations take the form

$$s = T(r)$$

where $s$ refers to the processed image pixel value and $r$ refers to the original image pixel value.
Negative images are useful for enhancing white or grey detail embedded in dark regions of an image.

- Note how much clearer the tissue is in the negative image of the mammogram below.

\[ s = 1.0 - r \]
Thresholding transformations are particularly useful for segmentation in which we want to isolate an object of interest from a background.

\[ s = \begin{cases} 
1.0 & r > \text{threshold} \\
0.0 & r \leq \text{threshold} 
\end{cases} \]
Intensity Transformations

Contrast stretching

Thresholding
Basic Grey Level Transformations

There are many different kinds of grey level transformations.

Three of the most common are shown here:

- **Linear**
  - Negative/Identity

- **Logarithmic**
  - Log/Inverse log

- **Power law**
  - $n^{th}$ power/$n^{th}$ root

The general form of the log transformation is

\[ s = c \times \log(1 + r) \]

The log transformation maps a narrow range of low input grey level values into a wider range of output values.

The inverse log transformation performs the opposite transformation.
Log functions are particularly useful when the input grey level values may have an extremely large range of values.

In the following example the Fourier transform of an image is put through a log transform to reveal more detail.

\[ s = \log(1 + r) \]
Power Law Transformations

Power law transformations have the following form

\[ s = c \cdot r^\gamma \]

Map a narrow range of dark input values into a wider range of output values or vice versa.

Varying \( \gamma \) gives a whole family of curves.
Power Law Example
Power Law Example (cont…)

\[ \gamma = 0.6 \]

\[ \begin{array}{cccccc}
0 & 0.1 & 0.2 & 0.3 & 0.4 & 0.5 \\
0.9 & 0.8 & 0.7 & 0.6 & 0.5 & 0.4 \\
0.8 & 0.7 & 0.6 & 0.5 & 0.4 & 0.3 \\
0.7 & 0.6 & 0.5 & 0.4 & 0.3 & 0.2 \\
0.6 & 0.5 & 0.4 & 0.3 & 0.2 & 0.1 \\
0.5 & 0.4 & 0.3 & 0.2 & 0.1 & 0.0 \\
0.4 & 0.3 & 0.2 & 0.1 & 0.0 & 0.0 \\
0.3 & 0.2 & 0.1 & 0.0 & 0.0 & 0.0 \\
0.2 & 0.1 & 0.0 & 0.0 & 0.0 & 0.0 \\
0.1 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\
0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\
\end{array} \]
Power Law Example (cont...)
Power Law Example (cont…)

\[ \gamma = 0.3 \]
The images to the right show a magnetic resonance (MR) image of a fractured human spine. Different curves highlight different detail.
Power Law Example
\[ \gamma = 5.0 \]
Power Law Transformations (cont…)

An aerial photo of a runway is shown
This time power law transforms are used to darken the image
Different curves highlight different detail
Many of you might be familiar with gamma correction of computer monitors. Problem is that display devices do not respond linearly to different intensities. Can be corrected using a log transform.
Rather than using a well defined mathematical function we can use arbitrary user-defined transforms.

The images below show a contrast stretching linear transform to add contrast to a poor quality image.
FIGURE 3.11 (a) This transformation highlights intensity range \([A, B]\) and reduces all other intensities to a lower level. (b) This transformation highlights range \([A, B]\) and preserves all other intensity levels.
FIGURE 3.12 (a) Aortic angiogram. (b) Result of using a slicing transformation of the type illustrated in Fig. 3.11(a), with the range of intensities of interest selected in the upper end of the gray scale. (c) Result of using the transformation in Fig. 3.11(b), with the selected area set to black, so that grays in the area of the blood vessels and kidneys were preserved. (Original image courtesy of Dr. Thomas R. Gest, University of Michigan Medical School.)
Bit Plane Slicing

Often by isolating particular bits of the pixel values in an image we can highlight interesting aspects of that image.

- Higher-order bits usually contain most of the significant visual information.
- Lower-order bits contain subtle details.
Bit Plane Slicing (cont...)

Figure 3.14 (a) An 8-bit gray-scale image of size $500 \times 1192$ pixels. (b) through (i) Bit planes 1 through 8, with bit plane 1 corresponding to the least significant bit. Each bit plane is a binary image.
Useful for compression.

Reconstruction is obtained by:

\[ I(i, j) = \sum_{n=1}^{N} 2^{n-1} I_n(i, j) \]
Let $g(x, y)$ denote a corrupted image by adding noise $\eta(x, y)$ to a noiseless image $f(x, y)$:

$$g(x, y) = f(x, y) + \eta(x, y)$$

The noise has zero mean value $E[z_i] = 0$

At every pair of coordinates $z_i = (x_i, y_i)$ the noise is uncorrelated

$$E[z_i z_j] = 0, \quad E[z_i^2] = \sigma^2_\eta$$
The noise effect is reduced by averaging a set of \( K \) noisy images. The new image is

\[
g(x, y) = \frac{1}{K} \sum_{i=1}^{K} g_i(x, y)
\]

The intensities at each pixel of the new image may be viewed as random variables. The mean value and the standard deviation of the new image show that the effect of noise is reduced.
Average image (cont...)

\[ E\left[\bar{g}(x, y)\right] = E\left[\frac{1}{K} \sum_{i=1}^{K} g_i(x, y)\right] = \frac{1}{K} E\left[\sum_{i=1}^{K} g_i(x, y)\right] \]

\[ = \frac{1}{K} E\left[\sum_{i=1}^{K} f(x, y) + \eta_i(x, y)\right] \]

\[ = \frac{1}{K} E\left[\sum_{i=1}^{K} f(x, y)\right] + \frac{1}{K} E\left[\sum_{i=1}^{K} \eta_i(x, y)\right] \]

\[ = \frac{1}{K} Kf(x, y) + \frac{1}{K} K0 = f(x, y) \]
Similarly, the standard deviation of the new image is

$$
\sigma_{\bar{g}(x,y)} = E \left[ \left( \bar{g}(x, y) \right)^2 \right] - \left( E \left[ \bar{g}(x, y) \right] \right)^2 = \frac{1}{\sqrt{K}} \sigma_{\eta(x,y)}
$$

As $K$ increases the variability of the pixel intensity decreases and remains close to the noiseless image values $f(x,y)$.

The images must be registered!
Average image (cont...)

Figure 2.26  (a) Image of Galaxy Pair NGC 3314 corrupted by additive Gaussian noise. (b)–(f) Results of averaging 5, 10, 20, 50, and 100 noisy images, respectively. (Original image courtesy of NASA.)
We have looked at different kinds of point processing image enhancement.
Next time we will start to look at histogram processing methods.