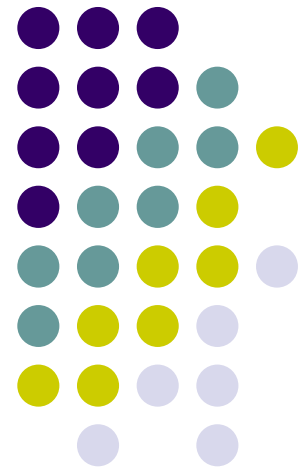
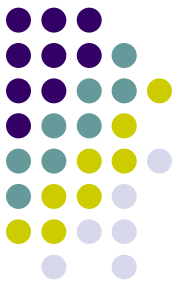


# Θέματα Εφαρμογών Βάσεων Δεδομένων : Ιδιωτικότητα Δεδομένων

## 4. Power Law Graphs

Ζαγορίσιος Παναγιώτης  
Πατσαϊκονόμου Χριστίνα

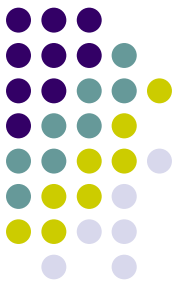




# Barabási-Albert (BA) Scale Free Model

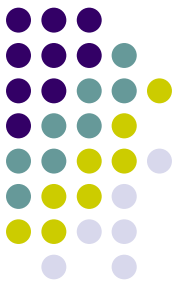
- Algorithm for generating random scale free networks (graphs) that they have **power law** (or scale free) degree distributions.
- Power law:  $P(k)=ck^{(\gamma-2)}$  : constant  $c$ ,  $2<\gamma<3$
- Two important general concepts:
  - **Growth**
  - **Preferential attachment**

Both growth and preferential attachment exist in real networks.



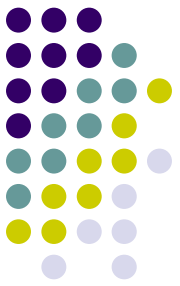
# Basic concept of BA model

- *Growth*: the number of nodes in the network increases over time.
- *Preferential attachment*: the more connected node is the more likely to receive new links. Nodes with higher degree have stronger ability to grab links added to the network.
  - For example, how connected people in a social network or on the web pages links such as Google, Wikipedia etc



# Parameters of algorithm

- Input
  - $n$ : # of nodes
  - $m$ : # of edges to attach from a new node to existing nodes
  - $seed$ : (int) for random number generator (default=None)
- Output
  - $G$ : Graph
- The initialization is a graph with no nodes and no edges.



# Basic steps of algorithm

1. Starting with an initial network (graph) with a few nodes. ( $\rightarrow$  growth)

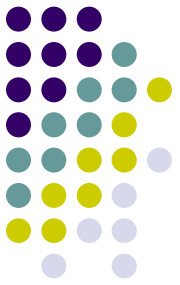
no: nodes of initialization ( $n_0 \geq 2$ )

mo: edges of initialization

Each of these nodes ( $n_0$ ) must have at least one connection (or fully connected). The final structure does not depend on the initial number of nodes.

2. At each time step, a new node is added. Older nodes with a higher degree have a higher probability of attracting edges from a new node. ( $\rightarrow$  preferential attachment)

# Connection probability



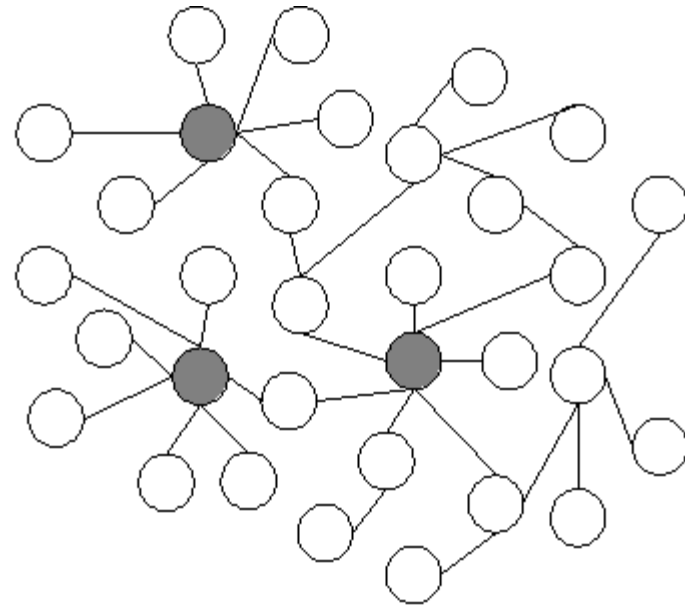
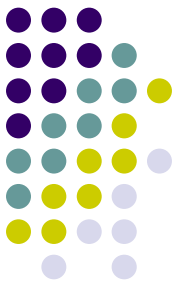
- Connection probability-Preferential attachment
- A new node will be connected to node  $i$  depends on the connectivity  $k_i$  of that node.

Probability of attachment is given by:

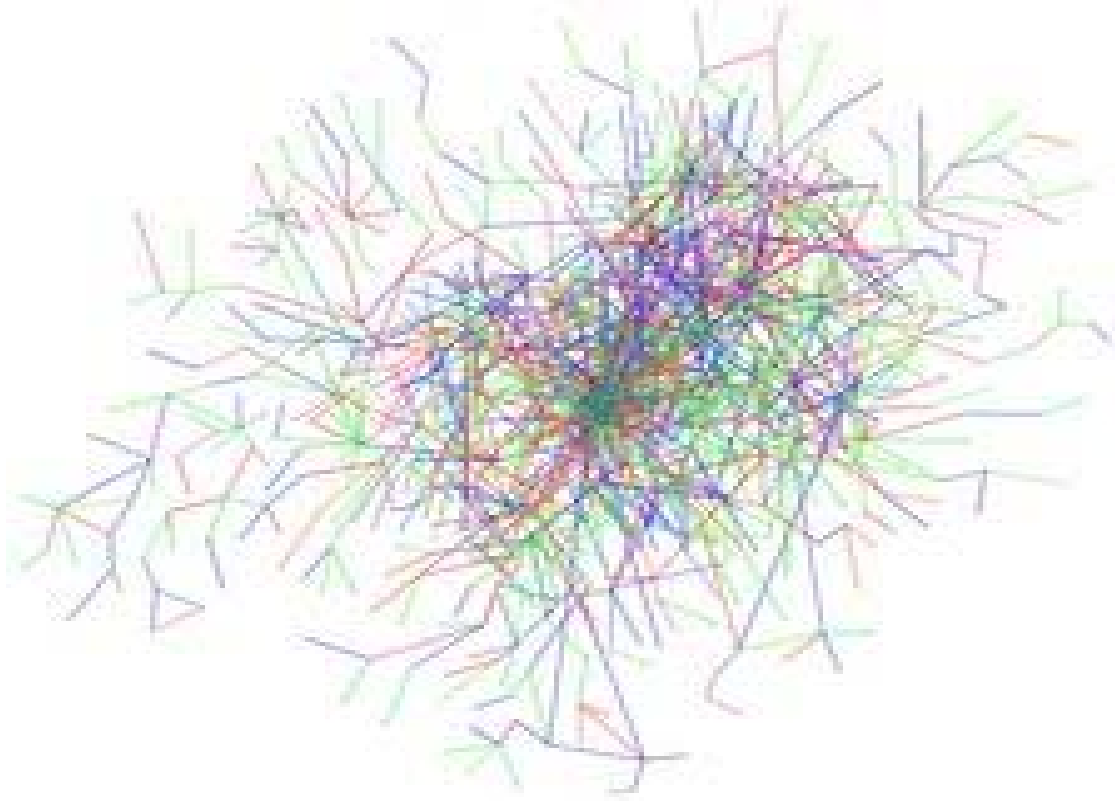
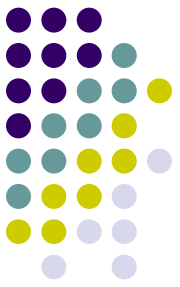
$$P(k_i) = k_i / \sum_i k_i$$

This can result in self-loops or multiple edges.

# 1<sup>st</sup> example of power law graph

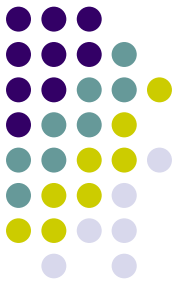


## 2<sup>nd</sup> example of power law graph



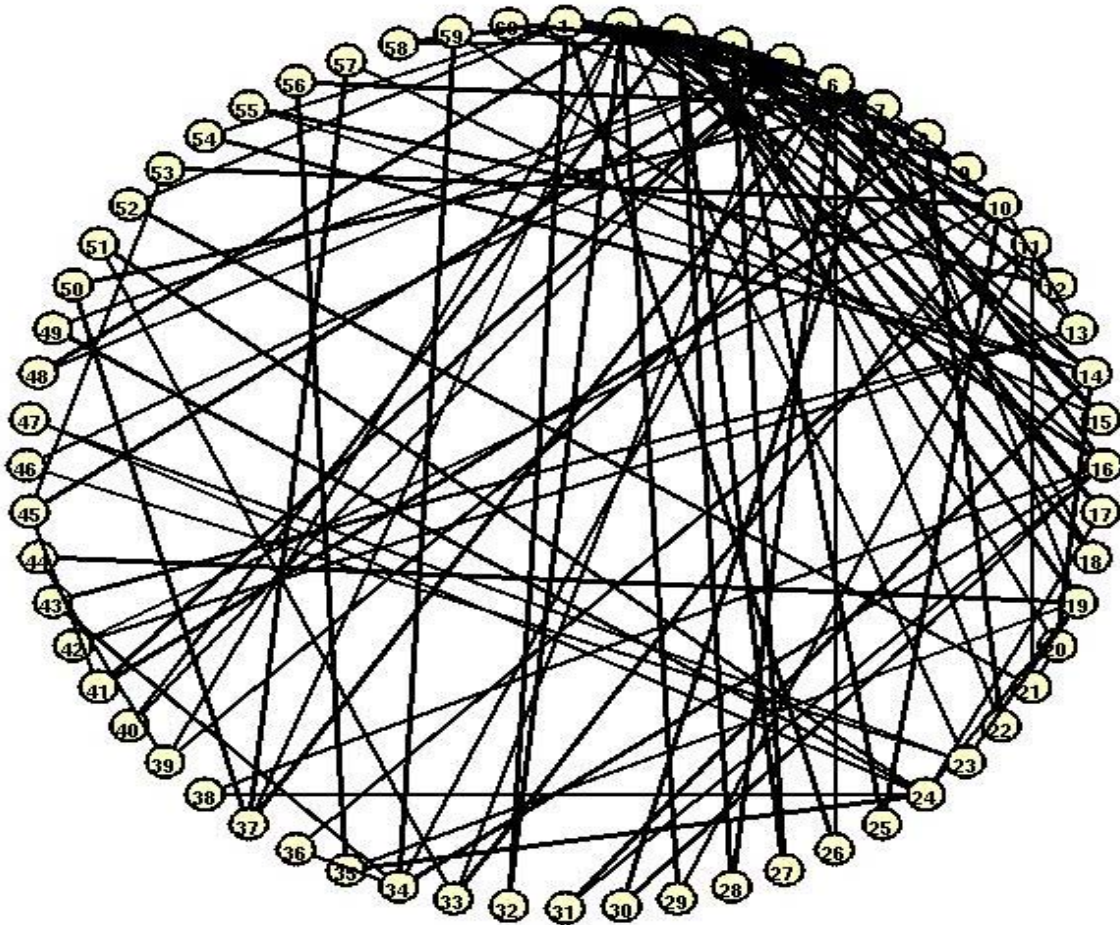


# Applications



- Applied to generate any undirected network
- Such as,
  - the collaboration network among scientist
  - the movie actor network
  - or other social networks in which connections between edges are undirected...

# Fully connected power law graph ( $n=60, no=6, m=2, mo=5$ )



# Non fully connected power law graph ( $n=60, no=6, m=2$ )

